

**OBJECT RECOGNITION USING  
SHAPE AND BEHAVIORAL  
FEATURES**

by

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# Abstract

Object Recognition is the domain of computer vision that deals with the classification of objects in two or three dimensions as instances of predetermined object classes, and is useful for image analysis and understanding. One of the most powerful properties used for recognition of objects is the shape of the object. Other features traditionally used include color, texture, moments and other attributes visible from single static images. The difficulty in obtaining error-free classification is that image data almost always has noise, is cluttered with many different objects and the objects may be occluded or hidden so only a fraction of the object is visible. That is why it is useful to consider additional information which is not available from single static images.

In this thesis we define and employ behavioral features along with shape features to characterize objects. We model the dynamic behavior of each object class by its common pattern of movement to help disambiguate different objects that may look similar but belong to different object classes in light of their distinct behavioral features. We show that for a simulated environment problem where we create a database of a mix of objects with small and large variations in shapes, sizes and behavior models, the error rate of the system that uses shape alone decreases from a top-choice error rate of 7-30% to a top-choice error rate of 2-3% using shape and behavioral features, with performance gain with the addition of behavioral features depending on the noise levels in cases where the shapes are similar but objects have different behaviors.

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# Contents

<b>1</b>	<b>Introduction and Problem Statement</b>	<b>8</b>
1.1	Background . . . . .	8
1.2	Objective . . . . .	8
1.3	Scope . . . . .	9
1.4	Limitations . . . . .	12
<b>2</b>	<b>Overview of Object Recognition</b>	<b>14</b>
2.1	Literature review . . . . .	14
2.2	Shape: recognition from static images . . . . .	15
2.3	Behavior: dynamic aspects of recognition . . . . .	16
2.4	Combining shape and behavioral cues . . . . .	16
<b>3</b>	<b>Background</b>	<b>18</b>
3.1	B-splines . . . . .	18
3.1.1	Introduction . . . . .	18
3.1.2	Preliminaries . . . . .	19
3.1.3	Uniform cubic B-spline . . . . .	20
3.1.4	Translational, rotational and scaling invariance . . . . .	24
3.1.5	End conditions and multiple vertices . . . . .	24
3.1.6	Closed curves . . . . .	24
3.2	Particle filters . . . . .	26
3.2.1	Introduction to particle filtering . . . . .	26
3.2.2	Kalman filter . . . . .	27
3.2.3	Non-Linear filters . . . . .	28
3.2.4	Particle filters . . . . .	29

3.2.5	Condensation algorithm . . . . .	31
3.3	Syntactic parsing rules . . . . .	34
3.4	Classifiers . . . . .	36
3.4.1	Artificial neural networks . . . . .	36
<b>4</b>	<b>Design Methodology</b>	<b>42</b>
4.1	Conceptual design of the classifier system . . . . .	42
4.2	Stepping through the system operation . . . . .	47
<b>5</b>	<b>Environment Setup and Test Cases</b>	<b>50</b>
5.1	Object Shapes and Paths . . . . .	50
5.2	Grammar rules . . . . .	53
5.3	ORMOT . . . . .	54
5.4	Test data generation . . . . .	54
5.5	Parameters . . . . .	58
5.6	Test cases . . . . .	60
<b>6</b>	<b>Results</b>	<b>61</b>
<b>7</b>	<b>Conclusions and Future work</b>	<b>74</b>
7.1	Conclusions . . . . .	74
7.2	Future work . . . . .	75

# List of Figures

1.1	Flight patterns . . . . .	10
3.1	Curve . . . . .	19
3.2	Approximate B-spline . . . . .	20
3.3	Piecewise linear curve . . . . .	21
3.4	B-spline curve . . . . .	22
3.5	Basis functions . . . . .	22
3.6	Four basis functions . . . . .	23
3.7	Multiple control vertices . . . . .	25
3.8	Collinear control vertices . . . . .	25
3.9	Closed curve . . . . .	26
3.10	Condensation algorithm . . . . .	33
3.11	Derivation tree . . . . .	35
3.12	Perceptron . . . . .	37
3.13	Multilayer neural network . . . . .	40
4.1	Work engine . . . . .	43
5.1	Objects . . . . .	52
5.2	First screen of ORMOT . . . . .	55
5.3	Second screen of ORMOT . . . . .	56
5.4	Third screen of ORMOT . . . . .	57
5.5	Data Generation . . . . .	58
6.1	Tracked corners of objects . . . . .	62
6.2	Tracked corners of objects with more noise . . . . .	63
6.3	Averaged object shapes . . . . .	63

6.4	True path of type 2 . . . . .	64
6.5	Path of type 1 . . . . .	65
6.6	Smoothed path of type 11 . . . . .	66
6.7	Smoothed path of type 2 . . . . .	67
6.8	Smoothed path of type 10 . . . . .	68

# List of Tables

6.1	NN training Table . . . . .	69
6.2	Accuracy Table 1 . . . . .	69
6.3	Accuracy Table 2 . . . . .	70
6.4	Accuracy Table 3 . . . . .	70
6.5	Accuracy Table 4 . . . . .	71
6.6	Accuracy Table 5 . . . . .	71
6.7	Accuracy Table 6 . . . . .	72
6.8	Accuracy Table 7 . . . . .	72
6.9	Accuracy Table 8 . . . . .	73
6.10	Accuracy Table 9 . . . . .	73



# Chapter 1

## Introduction and Problem Statement

### 1.1 Background

Object recognition is the process by which a system, biological or artificial, tries to classify or identify an object. In computer vision this identification has been done using different cues the most prominent of which has been shape, others being color, texture, moments, topology, etc. In most problem settings, shape is definitely one of the strongest cues that help identify the object. Typically, other cues help in identifying the object faster or favor approximate answers in case of shape ambiguities. For example, consider a purple apple - the human mind will be able to make out that the object has the shape of an apple (provided the shape of the object can be recognized) but the color is different from that of an apple. Shape, the dominant cue, persuades us that it is indeed an apple, albeit one with an unusual color.

### 1.2 Objective

Shape can be observed from static imagery. When video imagery is available, one can observe how the object moves over space and time. The dynamic characteristics that are associated with a given object class constitute its behavior. Behavior can be used as another cue to help identify an object.

This cue is particularly useful when the object cannot be seen clearly or the shape cannot adequately discriminate to provide us the information we need. It is critical to predetermine the behavioral pattern of the object to be identified if we have to use this cue, just as we must know the shape characteristics of an object class to use shape cues to aid recognition. The behavioral pattern can be converted to features which can be used, alone or in conjunction with shape features, to train the system to recognize the object.

### 1.3 Scope

Let us consider examples where the behavior cues could be useful for object recognition in order to illustrate why behavior is an important cue.

1. Consider a scenario where you are watching birds at some distance. Your task is to identify which bird is which type. For example, an ornithologist may require a labeled video or images indicating the bird types for his studies. If the birds look similar or are at some distance away so that the shape cannot be used effectively to classify the birds, we can still use their motion behaviors, sound or color to recognize them. Different species of birds do have characteristic motion patterns when observed closely as is illustrated in the Figure 1.1. These could be used to identify or classify the birds. Consider flight patterns identified at the Cornell Lab of Ornithology as shown. The report from which this figure is extracted further notes that ways of identifying birds include shape, field marks, posture, size, flight pattern and habitat. Besides the flight pattern, the posture can also be considered as a behavioral pattern.
2. It is often necessary, and sometimes critical, to distinguish various classes of aircraft by their radar returns: military, commercial passenger, cargo, or general aviation aircraft, and if military, fighter-interceptor, bomber or specialized counter-measure aircraft. Radar returns often do not contain adequate information to distinguish shape features sufficient to make the recognition. But a highly maneuver-

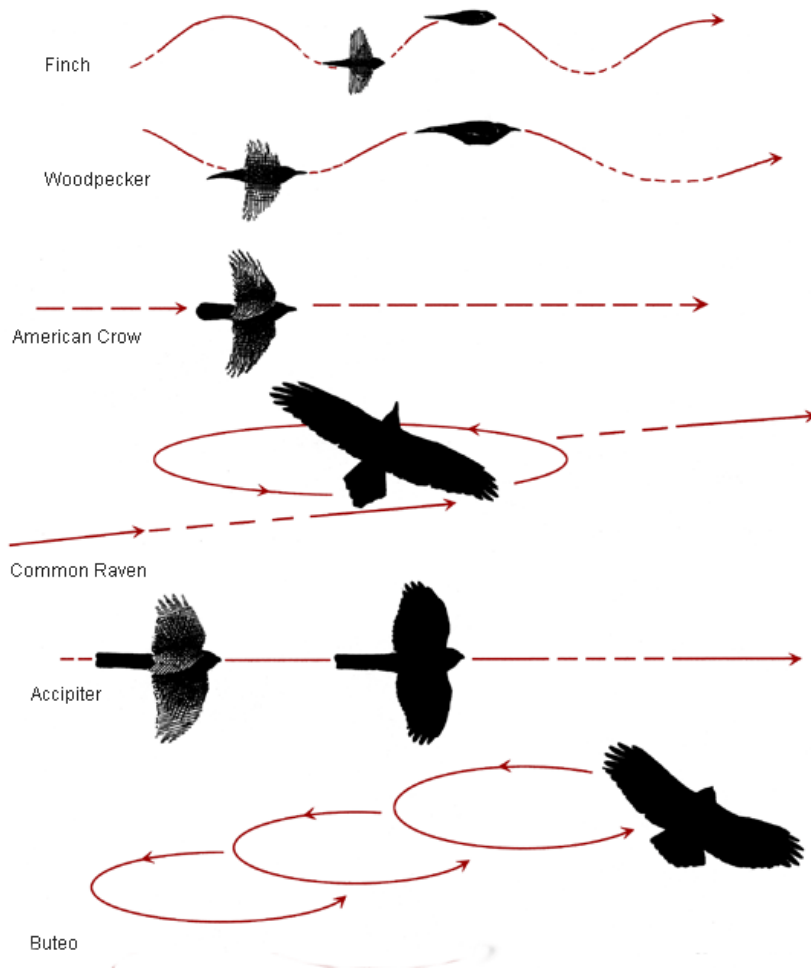


Figure 1.1: The different flight patterns of birds.

able fighter, for instance, can be easily distinguished from a lumbering bomber or wide-body passenger aircraft by its flight pattern. Simple behavioral cues such as airspeed can immediately disambiguate a jet aircraft from a single engine general aviation vehicle.

3. A similar example to differentiating between varieties of birds is to differentiate between different fish in the sea or between different schools of fish using their swim pattern. One would also be able to differentiate between different fish species which move at different speeds. Hence it can be possible to differentiate between a blue shark and the shortfin mako shark that moves faster in water. In addition, some species such as sharks swim with a side-to-side rhythmic motion, while others such as dolphins use an up-down rhythmic motion.
4. It would be possible to differentiate between whales and submarines through their motion and turns they take during movement.
5. During a day of heavy snow or rain, it is likely that the movement of a human may help us identify that it is a human as opposed to an animal. The snow or rain can distort the shape information.
6. Each person has a characteristic way of walking. When closely observed, this behavior can be used to some degree to help identify the person from a distance or from behind, and hence used as a biometric feature [1].
7. Consider a courier collecting and distributing packages in a locality. After observing that the person is going to several houses with boxes should give a cue as to what this person is doing and hence who he may be i.e. a courier. Here the shape information will be useless and it will become more difficult to identify the person type if the person is not clad in a recognizable uniform.
8. Consider a supermarket. We need to identify the shoplifters from the authentic shoppers. It will not be possible to differentiate between these classes unless we note what each of the individuals in the shop is doing. The shoplifter will be behaving in surreptitious ways, such as

putting things in his pockets without placing them back on the rack or in the cart. Nothing in shape or geometry could identify the shoplifter. Thus behavioral cues would be essential to disambiguate the normal shopper from the shoplifter [2], [3].

These are some of the examples where behavior can be used as an important cue that will aid in computer vision based object recognition. We discuss in our study the nature of behavioral cues, and how to extract behavioral features that can be used to support object recognition.

## 1.4 Limitations

Behavior cannot always be of great value in object recognition. There are limitations to the use of behavioral cues as well as favorable situations. Some common scenario characteristics that do not rely on behavior to recognize an object are:

1. The objects are stationary. A tree cannot be discriminated from a telephone pole by their behaviors.
2. Both the object types have same or similar behaviors. Actually, stationary behavior is a specific behavior, and item one above is a special case of this item. A fish can be discriminated from a rock in a stream by the rock's stationary behavior.
3. Objects don't follow the behavior pattern that was used to train the system. A shoplifter may behave as a legitimate shopper while he or she is in range of a security camera.
4. The behavior may be occluded by objects in front of it.
5. The shape and other features are so prominent that behavior may be unnecessary.

Hence when designing the object recognition system, we do not claim that behavior features are always necessary or even useful. But when video data is available, there are many circumstances in which behavior of object

classes can be modeled and recognition systems benefit by training to use behavioral cues in visual object recognition.

## Chapter 2

# Overview of Object Recognition

### 2.1 Literature review

Object Recognition deals with the recognition or classification of different objects in two or three dimensional images as instances of predetermined object classes. Object recognition is useful for image analysis and understanding. Shape [4] has been used as one of the most powerful features to recognize the object. There are other features that are also used like color [4],[5], texture [5], depth, topology, moments [6],[7], etc. that are derived from static images. More complex Bayesian methods and aspect graph methods are also used. Image data almost always has noise, is cluttered with many different objects and the objects may be occluded or hidden so only a fraction of the part is visible. Besides this the object may be present in any location, orientation and may be scaled in the image. Different parts of the image and hence the object may be illuminated differently and by different light sources. Considering all this variation and a multitude of possibilities would cause recognition systems to have high computational complexity, high decision latency and be vulnerable to error. Ideally, the recognition system should have scale, translation and rotation invariant algorithms, be robust to occlusions, noise and illumination differences, should be capable of capturing the containment relationship of parts of an object and should be

fast enough to be useful for use for real time applications. The system could also have specialized algorithms running in parallel for detecting specific features needed to enhance the performance of the system.

A lot of research has been done in object recognition. Different shape techniques are used for object recognition. [4] combines shape and color information for object recognition. [8] uses shape-from-shading techniques. Similarly shape-from-texture exist [5]. [9] uses shape contexts for shape matching. [10] uses wavelet transforms for shape matching that can be used for object recognition. [11] uses shape similarity aspect graphs. Shapes of the objects are not rigid and can change. Taking care of this change is discussed in [12]. [13] discusses how to use shadow shape curves for 3 dimensional object recognition. The most basic shape features for two dimensional objects are discussed in [14].

## **2.2 Shape: recognition from static images**

We consider the simple shape features that are used for 2D objects that are discussed in [14]. Some of these shape features include the moments of different orders. They include the boundary length, area and moment of inertia. The compactness of the object is derived from the area and boundary length. The number of holes in the object is also a property of the object. The area and boundary length are shape and rotation invariant but not scale invariant. Hence it would be necessary to normalize the image if these properties are to be used. The moment of inertia about the x, y and xy is also a useful property. To re-orient the object to a standard, the object can be rotated using the axis of minimum moment of inertia about xy. This can be done if the object is not symmetrical or if the ambiguities regarding more than 1 minimum values can be resolved. B-splines [15] can represent the shape of the object and after standardization of the object i.e. rotating and shifting to the origin, the coefficients can be used as shape properties.



## 2.3 Behavior: dynamic aspects of recognition

Behavior may be defined as the action or reaction of an object or organism usually in relation to the environment [16]. It can be conscious or unconscious, overt or covert and voluntary or involuntary [16]. The behavior we are interested in is that kind that is characteristic of specific object classes, which can be observed, and which can be used for training. Objects may move in characteristic patterns of movement. Such a type of behavior can be observed in many animals like the bees [17]. Quite some amount of work has been done to classify humans using the gait and periodicity [18], [19], [1]. Periodicity as a behavior has been exploited in most of the work [19], [20], [2], [21], [22]. Most of the strategies have been the use of hidden Markov models and classification of trajectories [19], [23], [18]. Also motion patterns have been extracted in the frequency domain as discussed in [24].

We don't want to restrict ourselves to periodic motion as a method of detection of behavior. Behavioral features can consist of ordered sequences of brief movements referred to as gestures, and gestures can in turn consist of lower level more primitive movements. For example for a bird that makes a wavy motion followed by 3 loops in the air as its characteristic behavior, we can say that the wavy motion is a high level gesture and a sequence of 3 loops is another high level gesture. The lower level behavior will consist of the small left or right turns it makes or the straight line motion. These sequenced gestures make up the dynamic aspects that may help characterize objects and hence can be employed as behavioral features useful for recognition of certain objects.

## 2.4 Combining shape and behavioral cues

Most of the object recognition systems documented in the literature rely on static features alone. In fact the shape features are used for tracking the objects [25]. Behavior in itself can aid in classification in cases where the objects have some particular distinguishable pattern but have noisy shape features or very similar shape features in which case the shape and behavior features can be combined to improve the performance of the system.

Demonstrating this by the design and testing of a recognition system which combines shape and behavioral features is the main research goal of this thesis.

## Chapter 3

# Background

In this chapter background material critical to the design methodology developed in the remainder of the thesis is briefly reviewed. Much fuller treatment of these topics is available in the cited references.

### 3.1 B-splines

Spline shapes contain the curves of minimum strain energy and hence are considered mechanically sound. They give better performance in shape modeling than polylines connecting points and other families of curves, and are the representational framework for modeling the bounding contours of objects employed in this study.

#### 3.1.1 Introduction

For curve drawing, we can either interpolate the curve so that the curve goes through all the points or approximate the curve where a limit is defined to the distance between curves and points and hence the curve does not go through all the points. If we would connect the points by lines instead of curves, it would result in irregularities, discontinuities of derivatives, waste of space for storage and difficulty in manipulation. In splines a curve is defined by piecing together a succession of curve segments hence it is termed as a ‘piecewise’ approach[15]. Interpolation is easier than approximation but lacks some desirable properties. Bezier introduced the technique of

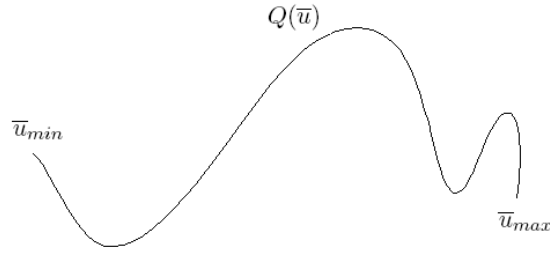


Figure 3.1: The curve  $Q$  showing  $\bar{u}_{min}$  and  $\bar{u}_{max}$ .

approximating using user-defined control points. Parametric B-splines have the advantage that we can control the degree of smoothness (continuity of derivatives) at the joints between adjacent curve segments independent of the order of the segments and number of control points. This level of control is not possible using Bezier curves, and motivates the use of B-splines to approximating the bounding contours for shape description.

### 3.1.2 Preliminaries

For a 2 dimensional curve, we can write the equation [15] of the curve as

$$Q(\bar{u}) = (X(\bar{u}), Y(\bar{u})). \quad (3.1)$$

$X$  and  $Y$  are single valued denoting the  $x$  and  $y$  co-ordinates. Similarly for a 3 dimensional curve we can add  $Z$  that will denote the  $z$  co-ordinates. The Figure 3.1 shows a curve with its parameter  $u$ . A single curve for  $X(\bar{u})$  and another for  $Y(\bar{u})$  will not produce a satisfactory curve. Hence we break the curve into a number of pieces called segments each defined by separate polynomials and join the segments to form a piecewise polynomial curve. Hence from the path of  $\bar{u}_{min}$  to  $\bar{u}_{max}$ , we get certain values of  $u$  called knots that are the joints between the polynomial segments  $\bar{u}_0, \bar{u}_1, \dots, \bar{u}_{min}, \dots, \bar{u}_{max}, \dots, \bar{u}_{last}$  which is the knot sequence or knot vector and  $\bar{u}_i \leq \bar{u}_{i+1}$  always. There is one polynomial piece between each  $\bar{u}_j$  and  $\bar{u}_{j+1}$  for  $X(\bar{u})$  and  $Y(\bar{u})$ .

The continuity constraints at the joints are important. If  $0th$  to  $dth$  derivative are everywhere continuous along the entire curve including the joints [15], then  $X$  and  $Y$  are said to be  $C^d$  continuous. Sometimes there are

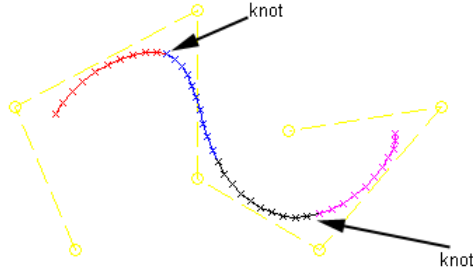


Figure 3.2: The approximate B-spline curve is shown with a few of the knot positions. The dashed lines show the sequence of control points used to create the B-spline curve.

multiple knots at the same point ( $\bar{u}_i = \bar{u}_{i+1}$ ) that cause the interval  $[\bar{u}_i, \bar{u}_{i+1}]$  to be vacuous for issues of continuity. However sometimes we will have all knots as distinct and a constant or uniform distance apart  $\bar{u}_{i+1} = \bar{u}_i + \delta$  and it is termed as a uniform knot sequence.

### 3.1.3 Uniform cubic B-spline

The B-spline is a curve created using the approximation method [15]. The uniform cubic B-spline has a uniform knot sequence and each segment is represented by a cubic polynomial. This spline has local control i.e. altering the position of a single data point (control vertex) causes only a part of the curve to change. This is computationally advantageous since we don't have to recompute the position of the entire curve if we only change a few points. The sequence of control vertices forms the control graph or control polygon.

A piecewise linear curve is shown in the Figure 3.3. In this the line connects the control vertices. The equation [15] for such a curve can be written as

$$\begin{aligned} Q_i(u) &= (X_i(u), Y_i(u)) \\ &= (1 - u)v_{i-1} + uv_i \end{aligned}$$

where  $v$  can be replaced by  $x$  for the  $x$ -coordinate equations and  $y$  for the  $y$ -coordinate equations. So changing  $V_i$  affects only  $Q_i(u)$  and  $Q_{i+1}(u)$ .  $v_{i-1}$

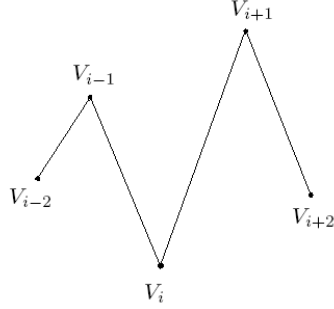


Figure 3.3: This is a piecewise linear curve where the control points are connected by straight lines.

and  $v_i$  scale a unit hat function whose max height is 1. In other words  $v_{i-1}$  and  $v_i$  is weighted by a corresponding unit hat function. The values of  $u$  are non-negative values and hence act as weights.  $v$ s on the other hand can have any positive, negative or zero value like scale factors. We can write the equations [15] as

$$V_i(u) = v_{i-1}B_{i-1}(\bar{u}) + v_iB_i(\bar{u}) \quad \text{for } \bar{u}_i \leq \bar{u} < \bar{u}_{i+1} \quad (3.2)$$

where

$$\begin{aligned} B_i(\bar{u}) &= \frac{\bar{u} - \bar{u}_i}{\bar{u}_{i+1} - \bar{u}_i} && \text{for } \bar{u}_i \leq \bar{u} < \bar{u}_{i+1} \\ &= \frac{\bar{u}_{i+2} - \bar{u}}{\bar{u}_{i+2} - \bar{u}_{i+1}} && \text{for } \bar{u}_{i+1} \leq \bar{u} < \bar{u}_{i+2} \end{aligned}$$

Hence at any point, that point is a linear combination of the functions  $B_i$  or as a weighted sum of the control vertices  $v_i$ . The unit hat functions  $B_i(u)$  are called basis functions.  $v_i$  contributes to the curve only where  $B_i(u)$  is non-zero. Since for  $v_i$ ,  $B_i(u)$  is non-zero over  $[u_i, u_{i+1})$  and  $[u_{i+1}, u_{i+2})$ ,  $v_i$  can influence only  $Q_i(u)$  and  $Q_{i+1}(u)$ . So in general we can write the equation of the curve [15] as

$$\begin{aligned} Q(\bar{u}) &= \sum_i v_i B_i(\bar{u}) \\ &= \sum_i (x_i B_i(\bar{u}), y_i B_i(\bar{u})). \end{aligned}$$

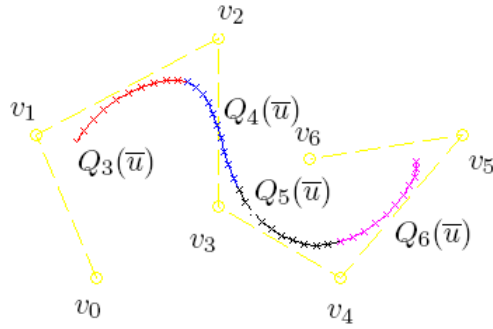


Figure 3.4: The curve figure shows the B-spline curve with the Q parts of the curve and the control graph.

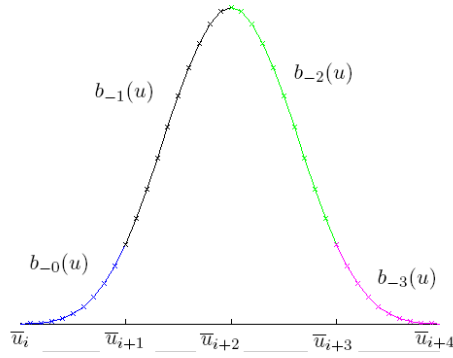


Figure 3.5: This figure shows the basis function with its four parts.

The basis functions for the piecewise cubic polynomial B-spline are shown in the Fig. 3.5. These are not scaled. They get scaled appropriately by the control vertices.

For control vertices 0 to  $m$  we need 4 basis functions to define the cubic curve segment i.e. there are 3 more control vertices than curve segments. In short, for  $m+1$  control vertices, there are  $m+1$  basis functions,  $m-2$  curve segments bounded by  $m-1$  knots and  $m-1+3+3 = m+5$  knots altogether. The curve is generated as  $\bar{u}$  runs from  $\bar{u}_3$  to  $\bar{u}_{m+1}$  with the conditions  $\bar{u}_0 < \bar{u}_1 < \bar{u}_2 < \bar{u}_3 = \bar{u}_{min}$ ;  $\bar{u}_{min} = \bar{u}_3 < \bar{u}_4 < \bar{u}_5 \dots < \bar{u}_{m+1} = \bar{u}_{max}$ ;  $\bar{u}_{max} = \bar{u}_{m+1} < \bar{u}_{m+2} < \bar{u}_{m+3} < \bar{u}_{m+4}$ .  $B(\bar{u})$  consists of 4 basis segments  $b_{-0}(u)$ ,  $b_{-1}(u)$ ,  $b_{-2}(u)$ ,  $b_{-3}(u)$  and each segment has the coefficients of the cubic

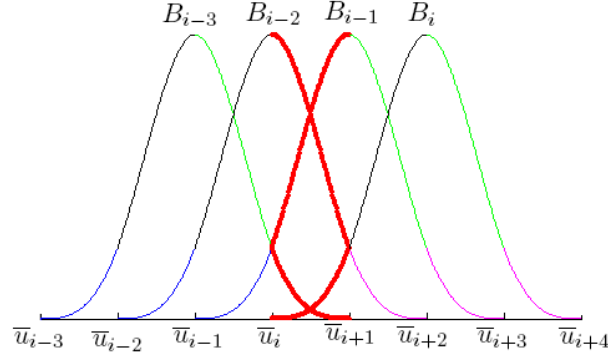


Figure 3.6: Four basis functions with their labels. The bold red section is the part that will be responsible for creation of one of the segment of the curve.

polynomial a, b, c and d. We need to determine 16 coefficients to determine  $B(u)$ . Also  $B_i(u) = 0$  for  $u \leq u_i$  and  $u \geq u_{i+4}$ . So the 1<sup>st</sup> and 2<sup>nd</sup> derivatives  $B_i^1(u)$  and  $B_i^2(u)$  are zero outside  $(\bar{u}_i, \bar{u}_{i+4})$ . Also the first and second derivatives match at each knot  $\bar{u}_j$ . We solve the equations [15] to give us the following results

$$b_{-0}(u) = \frac{1}{6}u^3 \quad (3.3)$$

$$b_{-1}(u) = \frac{1}{6}(1 + 3u + 3u^2 - 3u^3) \quad (3.4)$$

$$b_{-2}(u) = \frac{1}{6}(4 - 6u^2 + 3u^3) \quad (3.5)$$

$$b_{-3}(u) = \frac{1}{6}(1 - 3u + 3u^2 - u^3) \quad (3.6)$$

To determine a curve, we select a set of control vertices  $V_i$  and use them to define the curve given by the equation  $Q(\bar{u}) = \sum_i V_i B_i(\bar{u})$  and each  $B_i$  is simply a copy of B, shifted so that it extends from  $u_i$  to  $u_{i+4}$ .

$$\begin{aligned} Q_i(\bar{u}) &= \sum_{r=-3}^{r=0} V_{i+r} B_{i+r}(u) \\ &= V_{i-3} B_{i-3}(\bar{u}) + V_{i-2} B_{i-2}(\bar{u}) + V_{i-1} B_{i-1}(\bar{u}) + V_i B_i(\bar{u}). \end{aligned}$$

Replacing  $B_j(\bar{u})$  by the particular segment that pertains to the interval



$[u_i, u_{i+1})$ , we get the equation [15]

$$\begin{aligned} Q_i(\bar{u}) &= \sum_{r=-3}^{r=0} V_{i+r} b_r(u) \\ &= V_{i-3} b_{-3}(\bar{u}) + V_{i-2} b_{-2}(\bar{u}) + V_{i-1} b_{-1}(\bar{u}) + V_i b_0(\bar{u}). \end{aligned}$$

and is shown in the figure. Overall, for a uniform cubic B-spline, we have 3 fewer segments than we have control vertices.

### 3.1.4 Translational, rotational and scaling invariance

It is a desirable property that if we would shift or change the position of all control vertices by the same amount it would not affect the shape of the curve. This comes naturally to the curve and can be shown [15]. Similarly another desirable property is that if we would rotate all control vertices by the same amount it would not affect the shape of the curve. This also comes naturally to the curve and can be shown [15]. The scaling invariance is very similar to rotational invariance. Together they are equivalent to invariance under affine transformations.

### 3.1.5 End conditions and multiple vertices

To control the end control vertices, we can either repeat the end vertices  $V_0$  and  $V_m$  or create phantom vertices where ever we want so as to control the shape of the curve and can label those control points as  $V_{-1}$  and  $V_{m+1}$ . If we use multiple end vertices the shape of the curve changes depending on the number of multiple end vertices used. For example using 2 repeated end vertices causes the curve at the end to have a zero curvature while for 3 repeated end points, the curve interpolates between those end points (Figure 3.7). If 3 consecutive control points are collinear, then the curve passes through the middle control point as depicted in the Figure 3.8. If 4 consecutive control points are collinear, then the curve between the second and the third control point is a straight line as shown in the Figure 3.8.

### 3.1.6 Closed curves

If we repeat the first 3 vertices as the last 3 vertices of the control vector [15], the curve obtained becomes closed and continuous. This can be observed

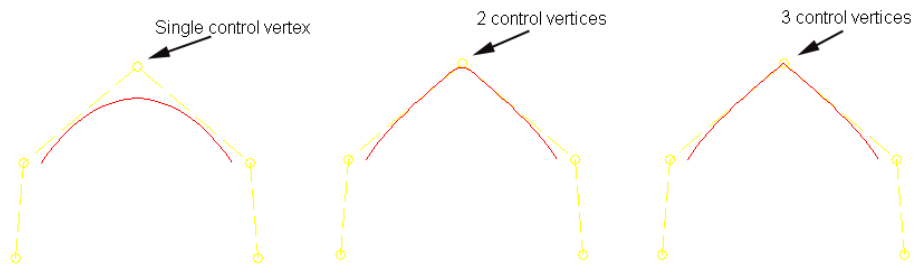


Figure 3.7: The effect of having multiple control vertices at the same point is seen in this figure.

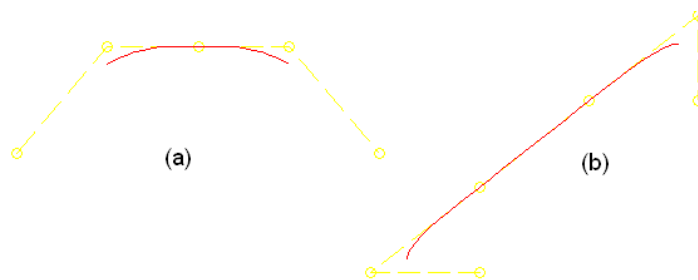


Figure 3.8: (a) The curve passes through the control vertex if the 3 consecutive control vertices are collinear. (b) The curve becomes a line through 2 control vertices if 4 consecutive control vertices are collinear.

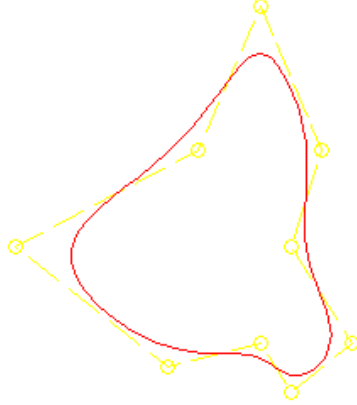


Figure 3.9: This is an example of a closed curve by repeating the first 3 vertices as the last 3 vertices in the control vector.

from the fact that  $P_{start} = \frac{V_0+4V_1+V_2}{6}$  and  $P_{end} = \frac{V_{m+1}+4V_{m+2}+V_{m+3}}{6}$  which turns out to be the same as the  $P_{start}$  equation. The Figure 3.9 shows such a closed curve.

## 3.2 Particle filters

### 3.2.1 Introduction to particle filtering

Stochastic filtering deals with estimating the distribution of a process given data up to the current time point [26]. If we use Bayesian statistics and Bayes rule for inference this filtering is called Bayesian filtering. We can estimate what the internal state  $x_n$  is, given the observations  $y_{0:n}$  with the goal of maximizing the a posteriori probability of our estimate. Stochastic filtering is often implemented recursively, updating the estimate of state at one time to the next time. In the case that the update is based on the current observation, this is referred to as recursive stochastic state filtering.

Recursive stochastic state filtering [27] may be generalized to the recursive estimation of state using only observations up to some earlier time (prediction), or up to some later time (smoothing).

1. *Filtering*: estimating the current state  $x_n$  given estimates of the previ-

ous states  $x_{0:n-1}$  and the current and previous observations  $y_{0:n}$  using process and measurement models

2. *Prediction*: (estimating a future state  $x_{n'>n}$  given earlier state estimates  $x_{0:n}$  and observations  $y_{0:n}$ )
3. *Smoothing*: finding  $x_{n'<n}$  given state estimates  $x_{0:n}$  and  $y_{0:n}$

The stochastic filtering problem in a dynamic state-space form [27] can be given by

1. *State equation*:

$$x_n = f(n, x_{n-1}, u_n, d_n) \quad (3.7)$$

where  $d$  denotes the process noise in the system and  $u$  denotes the system input vector in a controlled environment. The current internal state is a function of the current time, the previous internal state, the input vector (if in a controlled environment) and the process noise.

2. *Measurement equation*:

$$y_n = g(n, x_n, u_n, v_n) \quad (3.8)$$

where  $u$  denotes the system input vector in a controlled environment and  $v$  denotes the measurement noise. The observed state thus depends on the current time, the current internal state, the input control vector and the noise.

These equations reduce to the following if we neglect the input control vector:

$$x_n = f(x_{n-1}, d_n) \quad (3.9)$$

$$y_n = g(x_n, v_n) \quad (3.10)$$

### 3.2.2 Kalman filter

The Kalman filter [27], [28] is an optimal (minimum mean square error among its peers) recursive (needs previous data for predicting current state) data processing algorithm (filter) and used for a linear dynamic system with

the system having Gaussian noise (the probability density function has a bell shaped curve). The equations above reduce to

$$x_{n+1} = F_{n+1,n}x_n + d_n \quad (3.11)$$

$$y_n = G_n x_n + v_n \quad (3.12)$$

$F_{n+1,n}$  is the transition matrix while moving from state  $n$  to  $n+1$ ,  $G_n$  is measurement matrix in the current state and  $v_n$  and  $d_n$  are the noise in the system.

The Kalman filter [27] consists of the iterative predictor-corrector steps:

1. *Time update*: one step prediction of the measurement.
2. *Measurement update*: correction of the time update state estimate by propagating the conditional density given the observation.

The first order statistics (mean) and second order statistics (variance) fully determine a Gaussian density and the Kalman filter propagates both these (hence all information) without error to the next step. Note the optimality of the Kalman filter is limited to the linear Gaussian case.

### 3.2.3 Non-Linear filters

For non-linear or linear but non-Gaussian filtering [27], no closed form exact optimal solution can in general be obtained, the solution is infinite dimensional and hence the need to approximate. Approximate solutions to the nonlinear filtering problem have two categories: global methods (numerical approximation techniques used) and the local methods (linearization techniques or finite sum approximation).

The classes of non-linear filters can be enumerated [27] as:

1. Linearization method filters: Extended Kalman filter where the state equation and measurement equation are linearized and the posterior  $p(x_n|y_{0:n})$  approximated as a Gaussian.
2. Finite-Dimensional filters: Can be applied when the observations and filtering densities belong to the exponential class. This is usually performed with the conjugate approach where the prior and posterior are

assumed to come from some parametric probability function family.  
e.g. Daum filter, Benes filter and projection filter.

3. Classic partial differential equations (PDE) methods
4. Spectral Methods
5. Neural filter Methods
6. Particle Filters

The numerical approximation methods [27] include Gaussian/Laplace approximation, iterative quadrature, multigrid method and point-mass approximation, moment approximation, gaussian sum approximation, deterministic sampling approximation and Monte Carlo sampling approximation.

As the power of digital computers grow, non-linear non-Gaussian stochastic approximations based on sampling distributions which promise accuracy and robustness but at the cost of increased computational complexity have become attractive in many applications. In order to reduce the computation needs (associated with higher dimensionality and higher order moments), we need to represent the pdf as a set of random samples rather than a function over state space. For this purpose the sequential Monte Carlo methods [27] are used. Sequential Monte Carlo methods are used for parameter estimation (system identification) and state estimation (particle filters). Different kinds of Monte Carlo sampling methods exist that include importance sampling, rejection sampling, sequential importance sampling, sequential importance resampling (SIR), stratified sampling, Markov Chain Monte Carlo, Hybrid Monte-Carlo and Quasi Monte-Carlo. SIR in particular involves a resampling step inserted between two importance sampling steps to eliminate the samples with small importance weights and duplicate the samples with big weights thereby rejuvenating the sampler.

### 3.2.4 Particle filters

Sequential Monte Carlo is a kind of recursive Bayesian filter based on Monte Carlo simulation and is also called bootstrap filter. The working of the particle filter [27] can be summarized as follows:

The state space is partitioned as many parts, in which the particles are selected according to some probability measure with higher probability regions indicating more concentration of particles. The particle system evolves along the time according to the state equation with the evolving pdf determined by the Fokker Planck equation. Since the pdf can be approximated by the point-mass histogram, by random sampling of the state space, we get a number of particles representing the evolving pdf. However, since the posterior density model is unknown or hard to sample, we would rather choose another distribution for the sake of efficient sampling. The posterior distribution or density is empirically represented by a weighted sum of  $N_p$  samples drawn from the posterior distribution and when  $N_p$  is sufficiently large the approximate posterior approaches the true posterior. The weights can be updated recursively.

### **Sequential Importance Sampling (SIS) filter**

A problem that the ‘plain vanilla’ importance sampling filter faces is weight degeneracy or sample impoverishment. One of the solutions is to multiply the particles with high normalized weights and discard the particles with low normalized weights done in a resampling step. The effective sample size which is a suggested measure of degeneracy is compared to a predefined threshold to determine if resampling has to be done or not. The rejected samples are restarted and rechecked at the all previously violated thresholds.

### **Bootstrap /SIR filter**

The resampling done does not really eliminate the weight degeneracy problem [28] but saves much calculation time by discarding particles with insignificant weights. In the SIR filter the resampling is always performed. The posterior estimate is calculated before resampling because the resampling brings extra random variation to the current samples.

1. Obtain samples from the prior distribution
2. Importance sampling: draw samples approximately from  $p(x_n|x_{n-1})$

3. Weight update: calculate and normalize the weights  $w_n$  using the  $p(y_n|x_n)$
4. Resampling: generate  $N_p$  new particles from the old particle set using the weights obtained in (3)
5. Repeat 2 to 4.

The bootstrap filter algorithm [28] is given as follows:

If we have a set of random samples  $x_{n-1}$  the pdf  $p(x_{n-1}|y_{0:n-1})$ , the filter propagates and updates the samples to obtain the next  $x_n$ . The steps are similar to that described above:

1. Prediction: Use the state equation to get the new internal state  $x_n^*$
2. Update: On receiving the observation value  $y_n$ , obtain the normalized weight for each sample and resample  $N$  samples from the discrete distribution i.e. update the estimate of  $x_n^*$ .

The equation used is:

$$p(x_k|y_{0:k}) = \frac{p(y_k|x_k) * p(x_k|y_{0:k-1})}{p(y_k|y_{0:k-1})} \quad (3.13)$$

where the  $p(y_k|y_{0:k-1})$  can be considered as the normalizing constant.

There are many other filters like the improved SIS/SIR, condensation etc. [27].

### 3.2.5 Condensation algorithm

The condensation algorithm [29] can be used for tracking objects using a learned dynamical model along with observations. It is well suited to capturing shape information from video sequences, and has been employed in the combined shape-behavior recognition scheme to be described.

Condensation uses a technique called factored sampling [29] in an image sequence scenario. It is based on the SIR filter. It works better than the Kalman filter in environments with clutter and when the density is multimodal and hence non-Gaussian. The factored sampling algorithm generates a random variate  $x$  from a distributed probability distribution that approximates the posterior distribution  $p(x|z)$  where  $z$  represents the observation



and  $x$  represents the current state parameters. First the sample set is chosen using a prior density  $p(x)$  and then an index  $i \in 1, \dots, N$  is chosen with probability  $\pi_i$  where  $\pi_i = \frac{p(z|s^{(i)})}{\sum_{j=1}^N p(z|s^{(j)})}$ . If the number of samples  $N$  is increased, it approximates the posterior probability distribution better. Because of the use of particles or samples that represent a distribution, the object is represented as a distribution making it better off to deal with clutter than the Kalman filter. Moreover, when there are two similar objects in the environment, both the objects can be tracked since the condensation algorithm allows a multimodal distribution.

In the condensation algorithm, we can consider each time step to have a step of the complete factored sampling. In other words the factored sampling is applied at each time step. So first a prior density is chosen which has no functional representation and can have a multimodal probability density. It is derived from the sample set of the  $p(x_{t-1}|z_{t-1})$ . When the factored sampling is applied at each step, the output of the step is a weighted sample set with weights  $\pi$  each for a sample that denotes how important that sample is. This importance is used to resample so that the samples with insignificant weights can be thrown out or replaced by multiple copies of the samples with greater weight. When each sample is selected, it undergoes the deterministic drift and random diffusion and then the observation is used to generate the weights from the current observation density  $p(z_t|x_t)$  and hence the sample set.

The algorithm [29] can be described as follows:

Construct the  $N$  new samples as follows:

1. Select a sample  $s_t'^n$  as follows:
  - (a) Generate a random number  $r \in [0, 1]$  uniformly distributed.
  - (b) Find by binary subdivision, the smallest  $j$  for which  $c_{t-1}^j \geq r$
  - (c) Set  $s_t'^n = s_{t-1}^j$
2. Predict by sampling from  $p(x_t|x_{t-1} = s_t'^n)$  to choose each  $s_t^n$ . For instance in the case that the dynamics are governed by a linear stochastic differential equation, the new sample value may be generated as

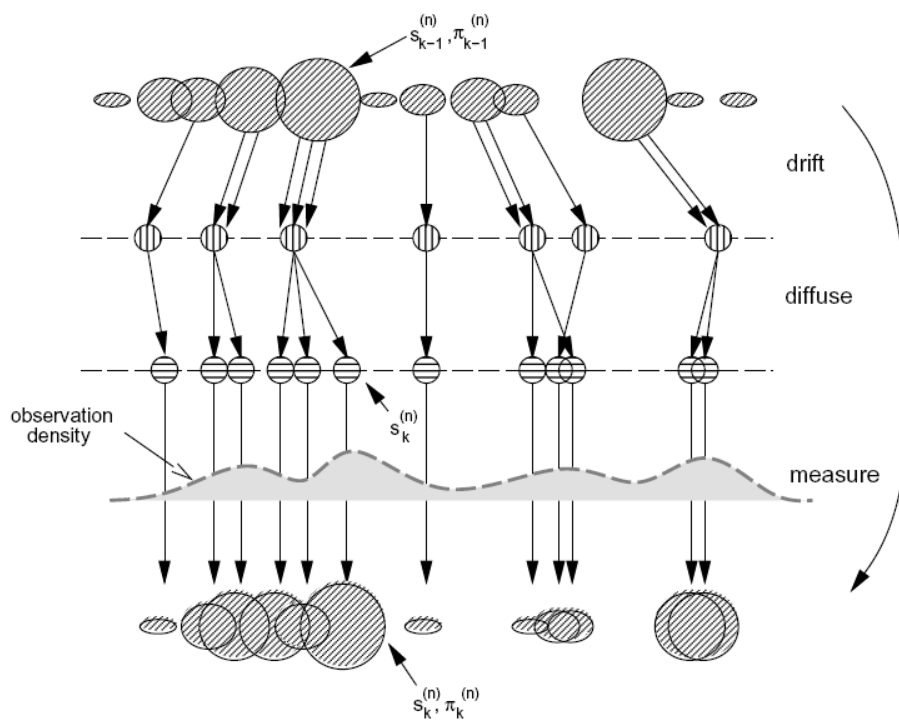


Figure 3.10: This is one step of the condensation algorithm. [29]

$s_t^n = As_t'^n + Bw_t^n$  where  $w_t^n$  is a vector of standard normal random variates and  $BB^T$  is the process noise covariance

3. Measure and weight the new position in terms of the measured features  $z_t$ :  $\pi_t^{(n)} = p(z_t|x_t = s_t^n)$ , then normalize so that  $\sum_n \pi_t^n = 1$  and store together with cumulative probability  $c$  as  $(s_t^n, \pi_t^n, c_t^n)$  where  $c_t^{(0)} = 0$  and  $c_t^{(n)} = c_t^{(n-1)} + \pi_t^{(n)}$  ( $n = 1, \dots, N$ )

If the shape of the object is also being found out, the equations for affine transformations can also be considered while tracking.

### 3.3 Syntactic parsing rules

The Condensation algorithm described in the previous section will be useful to monitor shape and determine short-term movement. A recognition system can be trained to detect specific short-term movements called gestures and tabulate sequential strings of gestures made by objects to be classified. Certain combinations of gestures make up characteristic behaviors of associated object classes. The mapping from gesture string to behavior in the proposed system is accomplished using syntactic pattern recognition.

Grammars are four-tuples containing a set of rules called productions which are compositions of terminal symbols and non-terminal symbols including a start symbol [30]. The grammars thus define associated languages, i.e. data structures that can be produced using the grammar. The productions can be written as  $A \rightarrow \alpha$ . Here we can replace  $A$  by  $\alpha$ . In this particular example,  $A$  is a string of non-terminals while  $\alpha$  is a string of both terminals and non-terminals.

The Chomsky Hierarchy [30] classifies grammars and hence languages in 4 types - Type 0 called unrestricted grammars, Type 1 called context sensitive grammars, Type 2 called context free grammars and Type 3 called Regular grammars. So in the case of the unrestricted grammars, the production rule can be written as  $\beta \rightarrow \alpha$  where  $\alpha$  and  $\beta$  is a string of any combination of terminals and non-terminals.  $\beta$  however cannot be an empty string. The empty string can be considered as a terminal symbol. There is no restriction on these grammars. For the context sensitive grammars, the

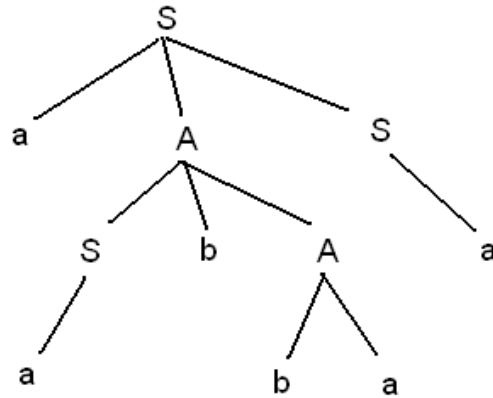


Figure 3.11: This is an example for the derivation tree as explained in the test for a context free grammar [30].

$A$  is of the form  $\beta B \gamma$  and the  $\alpha$  is of the form  $\beta \lambda \gamma$ . In other words the replacement of  $B$  by  $\lambda$  depends on the string before and after it and hence is called context sensitive.  $\alpha$  must have length greater or equal to that of  $A$ . In the case of context free grammars,  $A$  is only one non-terminal but  $\alpha$  is a string of terminals and non-terminals. The regular grammars have productions of the form  $A \rightarrow aB$  called right linear grammars or  $A \rightarrow Ba$  which are called left linear grammars.

We use the context free grammars [30] to obtain the behavioral patterns. The production rules are used for derivations i.e. when we replace the left part by the right part it is termed as a derivation. We can display the sequence of derivations as trees called derivation trees. Consider the grammar  $G = (\{S, A\}, \{a, b\}, P, S)$  where  $P$  is the set of production rules and consist of  $S \rightarrow aAS|a$  and  $A \rightarrow SbA|SS|ba$  and  $S$  is the start symbol,  $A$  is the other non-terminal symbol and  $a$  and  $b$  are terminal symbols. An example of the derivation tree can be given as shown in the Fig. 3.11. Two important normal forms in the context free grammars are Chomsky normal form and Greibach normal form [30] that may be useful while derivation.

## 3.4 Classifiers

Classifiers are basically systems that will differentiate or classify data to groups depending on the properties of the data. Learning systems can be classified as supervised learning, unsupervised learning and reinforcement learning. Supervised learning involves use of training data with known correct target or output values so as to allow the system to learn from examples. Unsupervised learning involves learning without any outputs labeled and is based more on clustering or grouping of data on dimensions that may help classify data. Reinforcement learning is that type where the system gets feedback from the environment in the form of rewards for useful actions that it does while interacting with the environment and punishment for poor actions. The system learns based on previous knowledge gained to make the current move in such a way to maximize the sum of future discounted rewards. There are different types of classifiers like the artificial neural network which is a supervised learning classifier, decision trees, support vector machines, k-means clustering and Linear discriminant analysis and so on. Since the classifier architecture selected for the present application is the neural net, we briefly discuss that classifier structure here.

### 3.4.1 Artificial neural networks

#### Introduction

Neural networks are models for learning functions. They are capable of learning from complex data to provide classification, among other functional goals. They are known to be very robust in approximating target functions and can train using data that has errors. The motivation behind creating artificial neural networks is the neural structure of all known natural intelligence. The human brain has approximately  $10^{11}$  neurons [31] and each of the neurons is connected to an average of about  $10^4$  other neurons to create a very complex network structure. The time taken for the working of one neuron in the brain is about  $10^{-3}$  seconds which is about  $10^7$  [31] slower than the fastest computer today. But because of the high amount of interconnections and the ability of each neuron to behave in itself, natural neurons

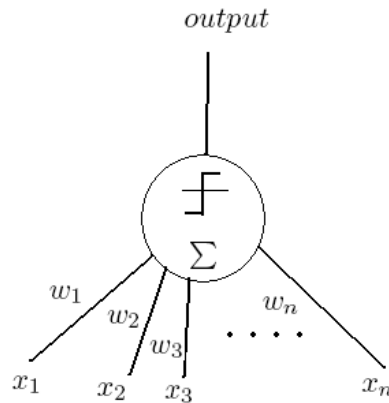


Figure 3.12: A single perceptron with inputs  $x_1, x_2, \dots, x_n$  and weights  $w_1, w_2, \dots, w_n$  and a single output.

can work together or in parallel which is a bottleneck in today's computers. Indeed, the human brain is capable of feats of pattern recognition, for instance recognizing faces that surpass the available supercomputers running the best algorithms in many instances.

### Representation

Each neuron [31] can be represented by inputs which correspond to the dendrites in actual neurons, outputs which correspond to the axon and the work unit or node which corresponds to the soma or body of the neuron. The outputs of the neuron can be connected to the inputs of other neurons if we build the multilayer neural network. A single neuron is shown in Figure and the multilayer neural network is shown in the Figure.

### Perceptron

The basic working of a perceptron is that the inputs are summed up each weighed by the weights of the neuron and the summed value is compared to the threshold [31]. If the summed value is greater than the threshold then the perceptron will output a 1 or else it will output a 0 or -1 depending on the threshold function you use. Normally, one of the input, the first or last input can be set to 1 so that the weight can act as a bias. Different

functions can be used for calculating the threshold values. Some examples are the sigmoid and the tanh functions. Thus the equations [31] can be given as

$$summed = \sum_{i=1}^n w_i x_i \quad (3.14)$$

The output is a function of the sum of the weighted inputs.

$$output = \sigma(summed) \quad (3.15)$$

The sigmoid function can be given as

$$\sigma(y) = \frac{1}{1 + e^{-y}} \quad (3.16)$$

Training of the neuron is basically updating the weights to more correctly classify the input data and thereby reducing the error. There are different algorithms that can be used for reducing this error and hence learning. Two of them discussed in [31] are the perceptron rule and the delta rule. The perceptron rule states that we should update the weight  $w_i$  by a factor  $\eta(t - o)x_i$  where  $\eta$  is the learning rate,  $t$  is the target or the correct classification,  $o$  is the output of the perceptron and  $x_i$  is the input. The perceptron fails to converge if the input data is not linearly separable. In which case, the delta rule should be used. The basic idea of the delta rule is to use a gradient descent approach. The weight error can be calculated using a suitable equation [31] like

$$E(w) = \frac{1}{2} \sum_{d=1}^n (t_d - o_d)^2 \quad (3.17)$$

where there are  $n$  training examples and hence  $t_d$  denotes the target value of the  $d$ th training example and  $o_d$  is the output of the perceptron of the  $d$ th training example. The plot of error on weight space shows the overall error and how gradient descent can be used to reach the global minima in that curve i.e. we try to move in a downward direction that will reduce the error. The weight update rule for  $w_i$  is given by  $\eta \sum_{d=1}^n (t_d - o_d)x_{id}$ . Perceptrons can be trained to represent some boolean functions like AND, OR, NAND and NOR but cannot represent XOR since the data for XOR is not linearly separable.

## Multilayer neural networks

Multilayer neural networks [31] have multiple layers of neurons so that the output of some neurons feed into the input of other neurons. The middle layers of neurons are called the hidden units while the output layer neurons are called the output units. Multilayer neural networks can represent highly non-linear data. The units generally represent non-linear functions and if we are to use gradient descent as the selected search method the threshold functions need to be differentiable. As mentioned earlier, the sigmoid or tanh functions which are differentiable can be used. The back propagation algorithm can be used for training multilayer neural networks.

The algorithm [31] which uses two layers of sigmoids can be given as follows:  
backpropagation(trainingData,  $\eta$ ,  $n_{in}$ ,  $n_{out}$ ,  $n_{hidden}$ )

The training data trainingData consists of the input data  $x$  as well as the target value  $t$ .

1. Create a feed-forward network with  $n_{in}$  inputs,  $n_{out}$  output neurons and  $n_{hidden}$  hidden neurons and initialize the weights of the neurons randomly.
2. Until the termination condition is met, Do For each of the trainingData tuple, Do
  - (a) Feed the input to the feed-forward network to get the output as  $o_u$  for every unit  $u$ .
  - (b) Propagate errors backward by updating the weights using the rules.

$$w_{ji} = w_{ji} + \Delta w_{ji} \quad (3.18)$$

where  $\Delta w_{ji} = \eta \delta_j x_{ji}$  and where the error term  $\delta$  for the output neuron  $k$  is given by  $\delta_k = o_k(1 - o_k)(t_k - o_k)$  and for the hidden unit  $h$  is  $\delta_h = o_h(1 - o_h) \sum_{k \in outputs} (t_k - o_k)$

Here a number of iterations are performed to achieve the amount of accuracy needed. During each iteration, the forward pass generates the outputs for the current weight settings of the neurons. Then the backward pass uses these outputs to calculate the error using the target information.



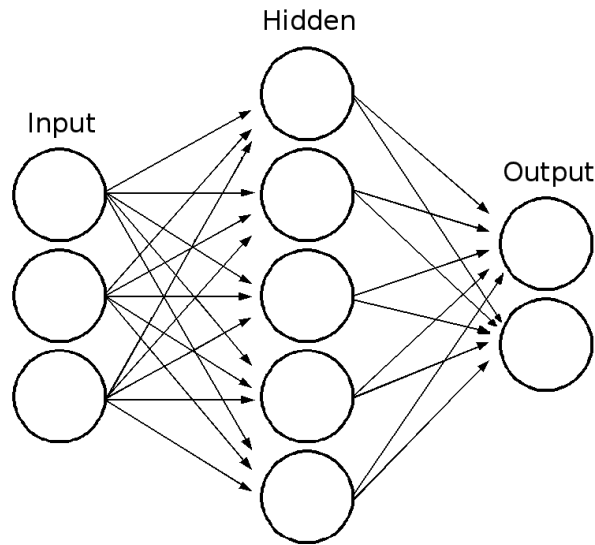


Figure 3.13: This is an example of a multilayer neural network with 3 inputs, 5 hidden neuron units and 2 output neuron units [32].

This error is used to update the weights of the neurons. The weight update is similar to the delta rule except that because of the non-linear nature, the weight update has extra terms that come from the differentiation of the functions. The sum in the hidden neurons update comes from the fact that each of the output neuron error can contribute to the hidden neuron error.

The multilayer neural network error surface can have multiple local minima and hence if the algorithm gets stuck in a local minima it may not produce correct results. The backpropagation algorithm also suffers from the problem of overfitting of training data. The training data may have noise and hence the data may not be a completely true representation of the ideal data. Hence when the neural network is trained it first tries to fit the data in general and as it is iterated for more time, the network tries to fit in the noise so as to reduce the training data errors. That is why the terminating condition for training is critical [31]. The terminating condition can be either a fixed number of iterations, or when the system reaches a particular accuracy of either the training data or the validation data. The validation data is not used for training but only to check the accuracy of the system over a validation set during training. So if the error over the validation set

starts increasing, the training can be stopped. A voting scheme can also be used as we have used in our system to be described in the next chapter in which more than one neural network is trained using the same training and validation data sets. So there are multiple sets of weights. During testing, each set of weight is applied and voting is used to obtain the correct classification.

## Chapter 4

# Design Methodology

This chapter details how the proposed recognition system which combines shape and behavior is designed. We can consider the complete system to consist of two parts. One is the data generation tool that is needed for our simulated environment in order to produce training and test data. The Fig. 5.5 shows how we generate this data and is discussed in the following chapter. The second, and more significant part, is that which inputs test or training data, extracts shape and behavior features and instantiates the learning system for classification. The Fig. 4.1 depicts the working of this system.

### 4.1 Conceptual design of the classifier system

The principal goal of this study is to define behavioral features of visible objects in video sequences and demonstrate their usefulness as adjuncts to shape features in classification. In this section, we specify classes of features, how they are to be parsed, and suggest a classifier suited to their use.

#### **Shape features**

Most key properties of the visible shape of objects are captured by their bounding contours. The tracking of these bounding contours in moving objects is a complex problem, especially in the presence of multiple object motions, noise, clutter and occlusion. Since the pdf's associated with these

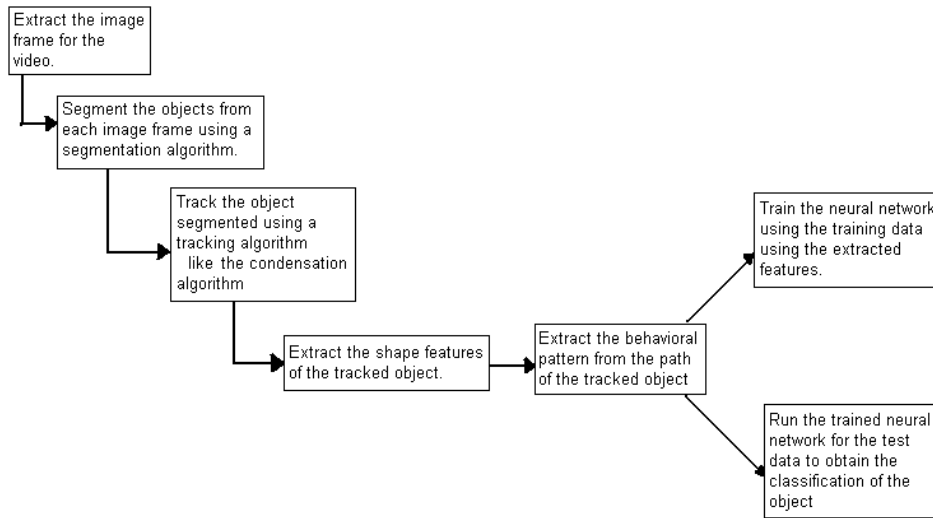


Figure 4.1: The shape and behavior based classifier

contours tend to be highly non-Gaussian, Kalman filters and their non-linear extensions are not generally useful. The Condensation algorithm, a bootstrap particle filtering approach, is more robust. Our design employs a Condensation filter to track the object of interest, and uses the coefficients of the B-spline segments as shape parameters. In addition, coarse scalar shape parameters such as area, boundary length, compactness and moment of inertia augment the B-spline coefficients.

### Behavior features

Useful behaviors are characteristic patterns of movement with differential correlation to object classes to be discriminated. Thus the same behavior can be attributed to two different object classes, but with different likelihoods, and be of value in classification. Each behavior can be modeled as the concatenation of simpler and shorter duration motion patterns we refer to as gestures. Thus the behavior of washing one's hands may consist of turning the faucet on the sink, reaching for soap, rubbing the soap into one's hands, thrusting one's hands under the water flow, rubbing the hands together, turning off the faucets, reaching for a towel, grasping the towel, rubbing one's hands on the towel, returning the towel. Each of the primitive actions is a

gesture, and together the ordered gestures are characteristic of the behavior.

While the identification of gestures depends upon the movement of the object bounding contour, minor variations must be accommodated within a gestural recognition class. For instance, in reaching for a towel the fingers can open sooner or later in the trajectory, and the hand may be rotated this way or that. Thus we select the centroid of the bounding contour at each time as a model of the object state sufficient for the purpose of gesture recognition. The bounding contour of the object is tracked and the centroid of the resulting object is used as the point representing the moving object. We capture the sequence of these points and use B-splines to smooth out the trajectory that is formed for noise reduction. Using predefined syntactic rules we capture the gestures from this trajectory.

To illustrate this process consider the use of simulated bird flights described in detail in the next chapter. We apply the Condensation algorithm to estimate the bounding contour in each frame, then map these down to the frame by frame motion of centroid which defines the trajectory. At each frame, the cumulative angle formed by the current trajectory point with the previous points is computed. If the angle is below a selected threshold, we declare the gesture to be motion in a straight line. If the angle signifies a left, right or back turn we label it so. We thus capture the gestures that are present in the trajectory. Higher level gestures are captured using syntactic rules applied to the string of lower level gestures thus discovered. For example the higher level gesture of rubbing ones hands while washing the hands may consist of lower level gestures of forcing the left hand over the right and another lower level gesture of forcing the right hand over the left repeated at least twice. The syntactic parsing is useful in capturing the true high-level gesture since variations of the sequence of the low-level gestures could signify that it is a different high-level gesture. Grammatical rules can be specified depending on the domain of the system as to how the high level gestures are obtained from the lower level gestures, and even the priority set over which high level gestures should be checked for first in a given stream of low-level gestures. In cases of highly stereotyped behavior, the rules can be quite strict permitting only exact sequences to be declared grammatical. In other cases, gesture classes could be formed by trajectories satisfying any

of a conjunction of weaker rules, or probabilistic syntactic approaches used.

### **A neural classifier**

We need a robust classifier for our object recognition system. It should be able to use both shape features as well as the behavior features. A natural choice for a classifier that uses only shape features is the neural network while that for a behavioral model is a hidden Markov model in which the hidden units correspond to high level gestures. However, we can also convert the low-level gestures to high-level gestures termed as behavioral features, in which case a single unified classifier can be used. This is what we choose for the classifier within this system. The required behavioral features, along with shape features, can be fed to a single integrated neural classifier.

We use two multilayer neural networks. One trains only on shape features. For test purposes, the number of shape inputs is 54, including area, boundary, compactness, moment of inertia and coefficients of the B-spline segments characterizing the bounding contour. The number of outputs depends on the number of objects selected in the study for classification. The other neural network trains on both the shape and behavioral features. It has 59 inputs made up of 54 shape features mentioned above and 5 behavioral features. The functions used are the logistic sigmoid in one layer and the softmax in the other layer. A voting scheme is used to resolve the problem where the network gets caught in a weak local minimum, and to bound the problem of overfitting. Ten voters are trained. Each voter's weights are saved. During testing, all voters express their classification. The maximum number of votes for a class is chosen as the correct classification of the object. In case of a tie, one of the classes with a plurality of votes is chosen at random. The selection of these specifications for the neural net classifier permits construction of a system for purposes of testing as described in the next chapter. In general, the parameters of the neural net design will be determined by the problem domain description.

## Assumptions

We make a few assumptions about the input data to the system to enable easier extraction of required features and design of the classifier. Simplifying assumptions are made on the premise that we can substitute for simpler modules in the system more complex ones which perform the same primary function as required to “build out” to more complex input data domains. Thus the system presented here should be considered as a proof of concept rather than a prototype or practical domain-specific design. The simplifying assumptions made are listed here.

1. The objects used are 2-D simulated objects. They are rigid bodies and have 6 corners. Each object has a different color. This is done to aid in tracking and segmentation. Segmentation is not the main concern of our work and we assume that as required, this can be replaced by a more powerful segmentation algorithm. The 6 corner points are chosen to facilitate tracking. Again we would replace the corner detection algorithm and tracking algorithm by more powerful ones in more complex cases.
2. There is only one object in a movie frame. Thus it becomes even easier to segment and we need not worry about the collision of the objects or occlusion. ORMOT, the software system we developed for testing and evaluation purposes as well as for generating the image and video data supports many objects in the movie frame. But in the reported training and testing, we restrict the number of objects to one for easier future processing. In applications involving multiple objects in single frames, the segmentation of the object to be classified would be assumed done in a pre-processing step.
3. The movement of the object from one time frame to the next is small enough to confidently track a given corner of each of the objects. In other words it is possible to observe one particular corner in the sequence without getting it confused with the other corners of the object or being subject to aliasing errors. This is necessary for symmetric objects with rotational motion components where due to rotational

symmetries the identity of corners of the object may otherwise be ambiguous.

4. We assume that there is some set of behavioral patterns that can be correlated with each of the object classes under study. For instance, if two classes of objects each have the same Brownian motion behavior, they cannot be disambiguated using behavioral cues. Such objects may have to be tracked for a longer duration of time so as to make sure that a fraction of its path that matches some other behavior pattern does not cause misleading results during classification.
5. For purposes of proof of concept, we also assume that each object has a set of exactly 5 high level gestures that will be visible in its movements over time for each training or test run. Though, practically we will want to extend that to a variable number, we do it here for simplicity of the learning system.
6. If the algorithm loses track of the object, we discard the entire reading and count that a recognition failure. In practice, the process and measurement noise for the test environment is set sufficiently small such that track was not broken on any training run.

## 4.2 Stepping through the system operation

The actual working engine as built for proof of concept testing can be described as follows:

1. Acquire the video or the image sequences of the object moving with time. If the video is obtained convert the video to time sequence image frames on which we can perform image processing.
2. From each image segment out the object. Use color as a feature for segmentation.
3. For the object, in time frame 1 image, extract the 6 corner points of the object. These can be obtained by using corner detection filters or using the Harris corner detection [33] algorithm. Apply condensation



algorithm and use these points obtained as the observation points. Obtain calculated values of the corner points from the condensation algorithm. In the next frame, repeat the procedure above. We use a simple linear motion model for the straight-line motion and use automatic model-switching for more complex behaviors like loops and waves. However the switching is done with reference to a time rather than more clever techniques. This part can be replaced by using the Bayesian mixed state approach as required. To find the correct corresponding corner points, shift the segmented object using the centroid to the centroid location of the object in the previous time frame, then find the closest corner points. Track using the condensation algorithm. You can note that the object may also be rotating and so we need to take care of that before using the points to extract shape features. So for each condensation algorithm calculated value, get the axis of minimum moment of inertia and rotate the object by that angle. The rotation is done using the cumulative sum of the previous rotation angles to take care of mismatch of the shapes of the object between time frames far apart and rotated by  $180^\circ$ .

4. Using these calculated values that are also shifted (centroid shifted to the origin) and rotated to the axis of minimum moment of inertia, draw a B-spline curve to approximate the shape of the object.
5. Extract the area, boundary length, compactness, moment of inertia about the x-axis, y-axis and xy-axis and the coefficients of the 6 curves that define the curves that form the shape a, b, c and d for both the x and y coordinates to get a total of 54 shape features.
6. If we are comparing the two systems one based on only shape features and the other using both shape and behavior features, check what the object is classified as by the neural network trained on only the shape features.
7. From the condensation algorithm calculated values, extract the centroid of the object. This is used to create the path along which the object is moving.

8. Approximate the path using the B-spline with the centroids as the control vertices.
9. Using the syntactic parsing rules, obtain the high level gestures from the low level gestures the object trajectory describes, and hence extract the behavioral features from them.
10. Feed the shape features and the behavioral features, a total of 59 features, to the neural network trained on both shape and behavioral features to see what classification this neural network gives.
11. Compare results obtained by the two different neural networks (shape alone vs. shape-behavior).

## Chapter 5

# Environment Setup and Test Cases

A simulated two dimensional environment was used for testing how well the behavioral system performs.

### 5.1 Object Shapes and Paths

The different types of objects we used included objects of similar shapes but different sizes as well as objects with very different shapes. We label the objects with type numbers for easy reference later in the test cases and results. Some of these objects are shown in the Fig. 5.1. These object descriptions include:

**Type 1** - Regular hexagon with a size of 1.0 units.

**Type 2** - Regular hexagon with a size of 1.2 units.

**Type 3** - Irregular hexagon with the longer side with a size of 1.5 units.

**Type 4** - Starship like shape.

**Type 5** - Starship like shape with a different angle.

**Type 6** - Starship like shape with yet another different angle.

**Type 7** - Three pointed star with an inner triangle side of length 0.5 units.

- Type 8** - Three pointed star with an inner triangle side of length 1 units.
- Type 9** - Regular hexagon with a size of 1.1 units
- Type 10** - Regular hexagon with a size of 1.05 units
- Type 11** - Regular hexagon with a size of 1.01 units
- Type 12** - Three pointed star with an inner triangle side of length 0.75 units.
- Type 13** - Three pointed star with an inner triangle side of length 0.6 units.
- Type 14** - Three pointed star with an inner triangle side of length 0.7 units.
- Type 15** - Regular hexagon with a size of 1.02 units
- Type 16** - Regular hexagon with a size of 1.03 units
- Type 17** - Regular hexagon with a size of 1.04 units
- Type 18** - Regular hexagon with a size of 1.005 units
- Type 19** - Regular hexagon with a size of 1.015 units
- Type 20** - Irregular hexagon with the longer side with a size of 1.49 units
- Type 21** - It is an irregular hexagon with the longer side with a size of 1.495 units
- Type 22** - Three pointed star with an inner triangle side of length 0.71 units.
- Type 23** - Three pointed star with an inner triangle side of length 0.72 units.
- Type 24** - Three pointed star with an inner triangle side of length 0.73 units.
- Type 25** - Three pointed star with an inner triangle side of length 0.74 units.

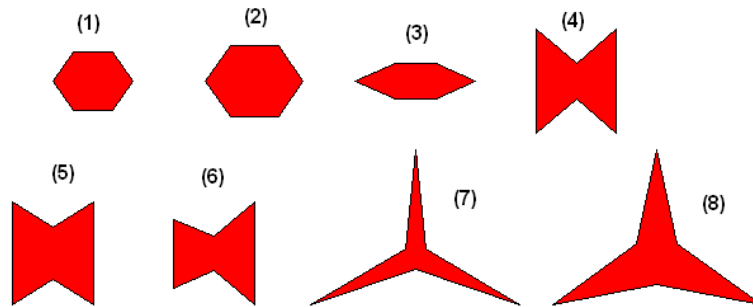


Figure 5.1: This figure shows a few of the objects used in our study. The number indicates the object type discussed in the text.

The objects also have behavioral patterns associated with them. Inspired by the bird flight behavioral dataset illustrated in Fig. 1.1, we create a set of different paths with can be associated with the object during system testing. This allows for a larger variety of object shape and behavior combinations. The object paths also have being designated type numbers. Each is made up of 5 behavioral features. For most of the them, the start and end features are straight lines. This helps us be sure of the features that are extracted. Some of the paths generated and/or tracked are shown in Figs. 6.4 - 6.8. The object path descriptions include:

**Type 1** - straight line, right loop, right loop, right loop, straight line.

**Type 2** - straight line, right loop, wave, left loop, straight line.

**Type 3** - straight line, left loop, left loop, left loop, straight line.

**Type 4** - straight line, wave, left loop, wave, straight line.

**Type 5** - straight line, right loop, left loop, right loop, straight line.

**Type 6** - straight line, right loop, wave, left loop, straight line.

**Type 7** - straight line, left loop, left loop, right loop, straight line.

**Type 8** - straight line, left loop, wave, left loop, straight line.

**Type 9** - straight line, wave, straight line, wave, straight line.

**Type 10** - straight line, wave, straight line, right turn, straight line.

**Type 11** - straight line, back turn, straight line, wave, straight line.

**Type 12** - straight line, left loop, straight line, left turn, straight line.

In each case, a recursive generative model for the ideal trajectory is used, and Gaussian white noise added at each step. Thus, as can be seen in Fig. 6.4, a straight line segment of the trajectory tends to drift from its original bearing, actually describing a random walk around its noise-free bearing. This models the influence random wind gusts might have on a bird's flight line when it is intent on flying straight.

## 5.2 Grammar rules

We define the grammatical rules for extracting the behavioral features. Small letters stand for terminal symbols and include d for long distance straight line, s for short distance straight line, b for back turn, l for left turn, r for right turn, p for hovering effect and e stands for a null. Capital letters stand for non-terminals and include C for Path, B stands for a back turn, L for left turn, R for right turn, P for hovering effect, W for wave, T for right or left loop. D, E, F, G, H, K and J are other intermediate non terminals. The rules can be given as follows

$$C \rightarrow d \mid H \mid e$$

$$H \rightarrow KdLdRdK \mid KdRdLdK \mid K$$

$$K \rightarrow JdLdJ \mid JdRdJ \mid JdLs \mid sLdJ \mid JdRs \mid sRdJ \mid sLs \mid sRs \mid e$$

$$J \rightarrow JdJ \mid D \mid e$$

$$D \rightarrow DTD \mid DWD \mid E \mid e$$

$$E \rightarrow EBE \mid F \mid e$$

$$F \rightarrow FLF \mid FRF \mid G \mid e$$

$$G \rightarrow s \mid e$$

$$B \rightarrow ll \mid lsl \mid lpl \mid rr \mid rsr \mid rpr$$
$$L \rightarrow l$$
$$R \rightarrow r$$
$$T \rightarrow l\{s,p\}l\{s,p\}l\{s,p\}l \mid r\{s,p\}r\{s,p\}r\{s,p\}r$$
$$W \rightarrow Wl\{s,p\}r\{s,p\}l\{s,p\}r\{s,p\}l\{s,p\}r\{s,p\} \mid \\ Wr\{s,p\}l\{s,p\}r\{s,p\}l\{s,p\}r\{s,p\}l\{s,p\} \mid e$$

### 5.3 ORMOT

ORMOT is a simulation environment created for demonstration purposes and for creating test data that may consist of image frames or a video. The 3 screens of this system are shown in Fig. 5.2, 5.3 and 5.4. We can have many objects moving in the screen as shown in the 3rd screen. ORMOT provides options including whether you want to create a video file, what are the screen dimensions you prefer for the path of the objects that will be simulated, the noise parameters associated with the object, the choice of objects and the different paths, start positions of the objects, for how much time you want the objects to move and color of the objects. It also has options of saving commonly used configurations for faster use later.

### 5.4 Test data generation

We explain the test data generation as depicted in Fig. 5.5 as follows:

1. We need to select the objects we would like in our setting. Each object will have its own shape. And each object will have some behavioral pattern of movement. Select the amount of noise variation you would like to have as the object moves. For e.g. to take into account the wind blowing when a bird is flying can be considered as noise. Select the noise variation in capturing or observing the object. Select the noise variation in the shape of the object that can be caused by the segmentation of the object.

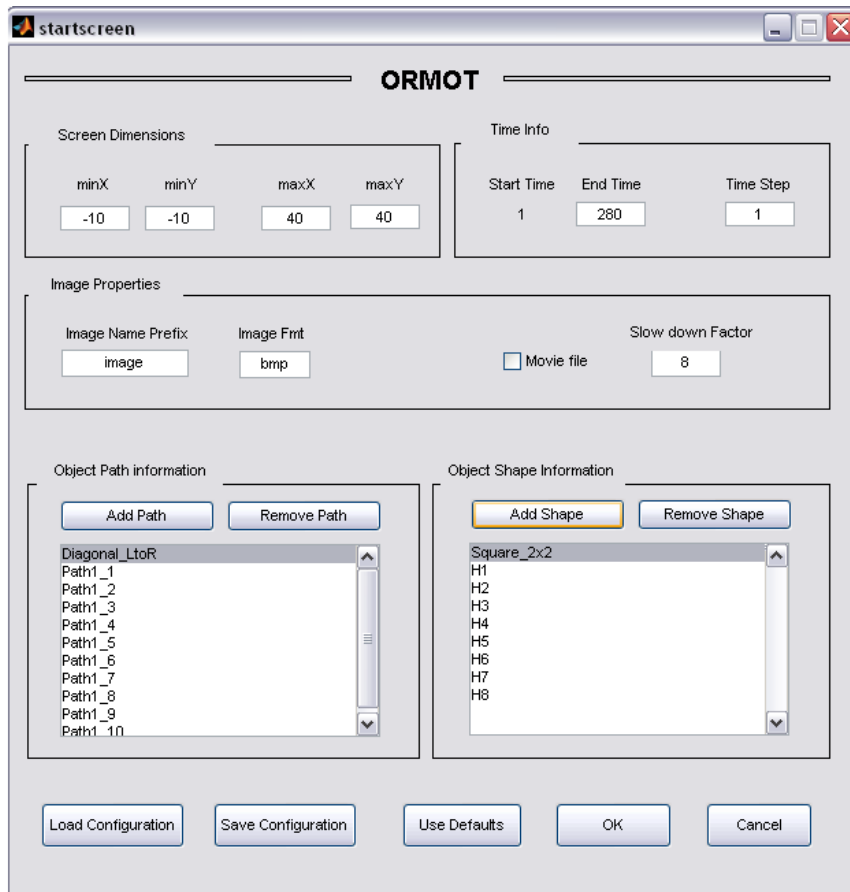


Figure 5.2: This is the screenshot of the first screen of ORMOT that was created for demonstrating the path movement and shape changes of the objects and creating images which can be used for tracking. Different parameters can be set and different paths and object types can be loaded.



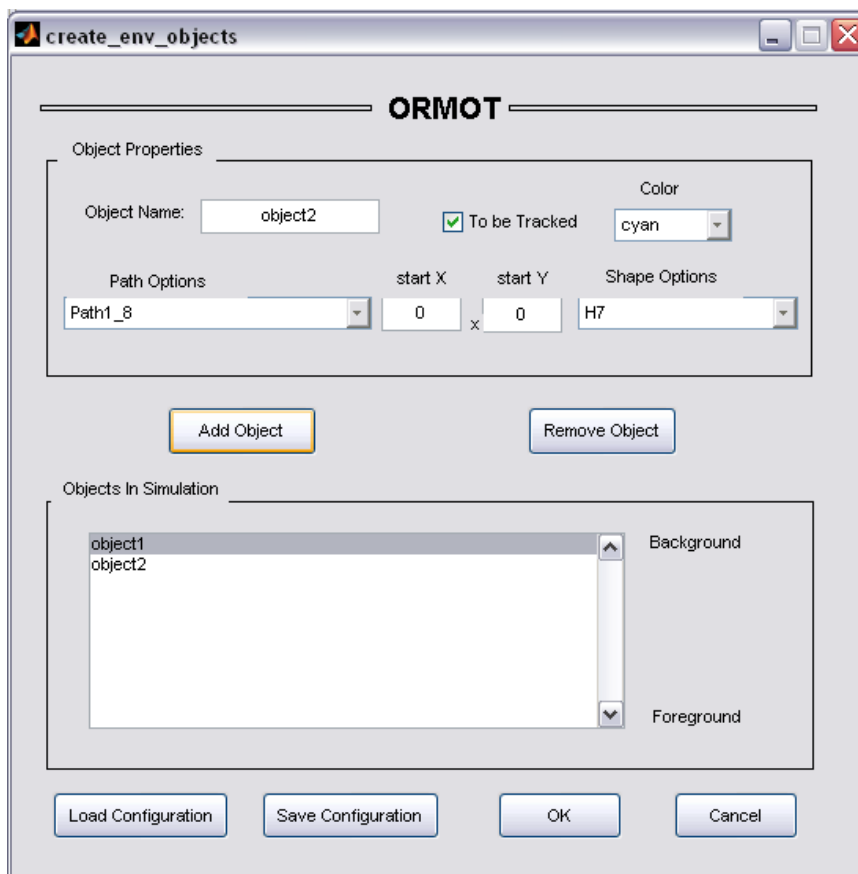


Figure 5.3: This is the screenshot of the 2nd screen of ORMOT. The objects can be selected and a path associated with them.

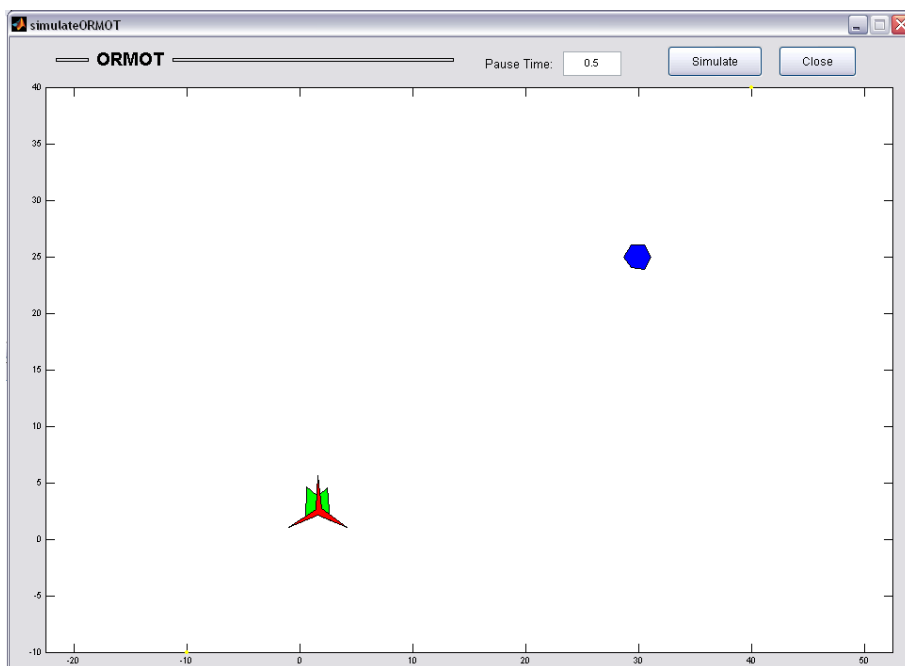


Figure 5.4: This is a screenshot of the third screen of ORMOT which displays the objects moving. Here we can see 3 objects one of which is occluded by the other.

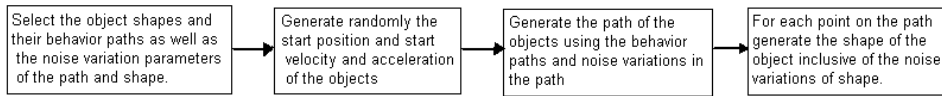


Figure 5.5: This figure shows how test and training data is generated.

2. Generate the location of the start point of the object randomly. Also randomly generate the initial velocity and acceleration of the object. We set the initial speed to be a constant so as to manage to get the objects entire behavioral pattern in one screen. Note that the initial directions of movement are random.
3. Generate the path of the object using the equations of motions and noise variations selected.
4. For each point on the path, generate the corner points of the object which are variable due to the shape noise added. Note that the centroid of the object is along the point of path selected.
5. We can capture the entire motion of the objects as a sequence of images or as a single video.

## 5.5 Parameters

Some of the important parameters are noted here. These parameters may have to be changed depending on the domain of the training data that is used or for faster processing or more accurate tracking.

1. **Shape noise standard deviation** is the amount of noise you want in the shape of the object. This parameter can be adjusted so as to take into account non-rigid body motions or the degree of clutter in the simulated environment. It also sets the noise during rotation of the objects. We vary it between 0.05 to 0.25 for different studies.
2. **True path noise standard deviation** is the amount of noise we would like to add to a perfect motion system. In reality every motion of the object is affected by the environment when it is moving may it be

friction or air resistance or even the malfunctioning body of the object for e.g. when a bird is hurt or is not able to flap its wings properly, the motion of the bird will be affected. These types of disturbances can be modeled by this parameter. We vary it between 0.05 to 0.1 for different studies.

3. **Observation noise standard deviation** is the parameter to take into account the noise of the instrument or camera capturing the images as well as the segmentation algorithms. Since we do not actually perform the segmentation on images, we use this parameter to take into account the errors that may have been caused by it. We vary it between 0.025 to 0.075 in our studies.
4. **Number of corner points** in the object is currently set to 6. We can set the number of corner points to a variable value with a few changes to the existing system and by normalizing the averaged shape of the object.
5. **Number of particles** in the condensation algorithm can be changed. Increasing the number of particles may possibly increase the accuracy of the system up to a limit but the computational complexity of the algorithm is linear in the number of particles. We used 100 particles in our study.
6. **Lengths and Angles** used in the grammar rules for extracting the behavioral features. The length for a long straight line is defined to have a threshold of 10 units. A left is defined to have a threshold angle of  $+75^\circ$  but not greater than  $+135^\circ$ . A right is defined to have a threshold angle of  $-75^\circ$  but not less than  $-135^\circ$ . A back turn is defined to have an angle turn less than  $-135^\circ$  or greater than  $+135^\circ$ . The decision of a turn is based on the cumulative angle for the last five sample points extracted from the path. Every tenth point in the B-spline curve corresponding to the smoothed path is chosen as the sample point for determining the length and angles.
7. **Eta** is the learning rate of the neural network. It was set to about 0.001 for most of the studies after observation of the fact that for our

data having a smaller value drastically reduced the speed by increase in the number of iterations for no benefit of increase in accuracy.

8. **Hidden neurons** of the multilayer neural network was set to 5 after observation that 3 under-represented the data and 7 had no improvement in the accuracy of the system.
9. **Number of voters** was set to 10.

## 5.6 Test cases

The goal in choosing the test cases was to show under which circumstances the addition of behavioral features would improve the accuracy of the object recognition and under which the additional features would act mainly as noise instead. With this in mind, 9 test groups were made. Each of these groups had variations in the noise parameters.

The first test group includes the case where there are 6 objects, all regular hexagons with slightly different sizes (a difference ratio of 0.01) but have significantly different behavior patterns. The second has these objects moving with exactly the same behavior pattern. The third and fourth are similar to the above respectively except that there are 5 objects and that the difference in sizes is even less (a difference ratio of 0.005), making the objects extremely difficult to classify accurately just using shape cues. The fifth has 4 objects that have shapes like stars and a difference of size of 0.01 and moving with different patterns while the sixth has the 4 objects moving in the same behavioral pattern. The seventh test group consists of 3 objects that are different in shape and have different behaviors. The eighth has 7 objects that have completely different shapes and different movement patterns while the ninth has the 7 objects moving in the same behavioral pattern.

The type number of the object and path of these test cases is shown in the Tables in the following chapter. Other details such as the size of training data and test data are also provided.

## Chapter 6

# Results

The following figures show us a few of the results obtained by generating paths considering noise, tracking of the objects using the condensation algorithm and the extraction of the shapes from the tracked object.

These are the definitions of the acronyms used in the tables that follow.

**Iter** Maximum iterations training data was trained up to an accuracy of 96% or 20000 iterations whichever is minimum.

**SNS** Shape Noise Sigma value

**TNS** True Noise Sigma value

**ONS** Observed Noise Sigma value

**SErr** Shape System misclassification

**SA %** Shape System accuracy percentage

**BErr** Behavioral System misclassification

**BA %** Behavioral System accuracy percentage

**eta** learning rate of the neural network

**HN** number of hidden neurons

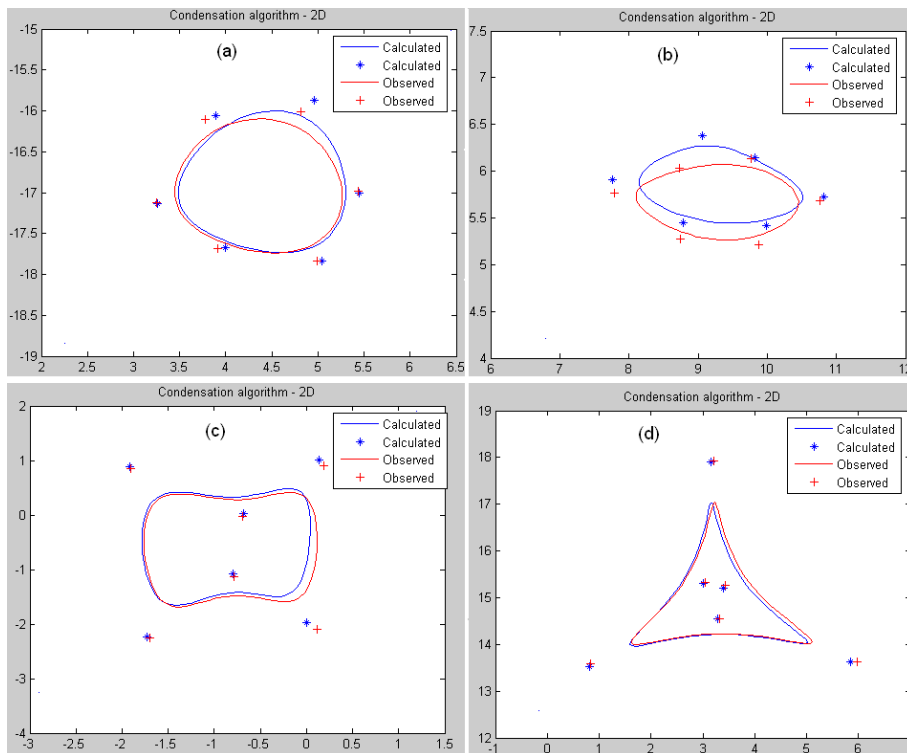


Figure 6.1: This figure contains 4 objects that show the object corner points as observed and as tracked with the help of the condensation algorithm. The shape noise sigma value was 0.1. (a), (b), (c) and (d) are the objects of type 1, 3, 5 and 7 respectively.

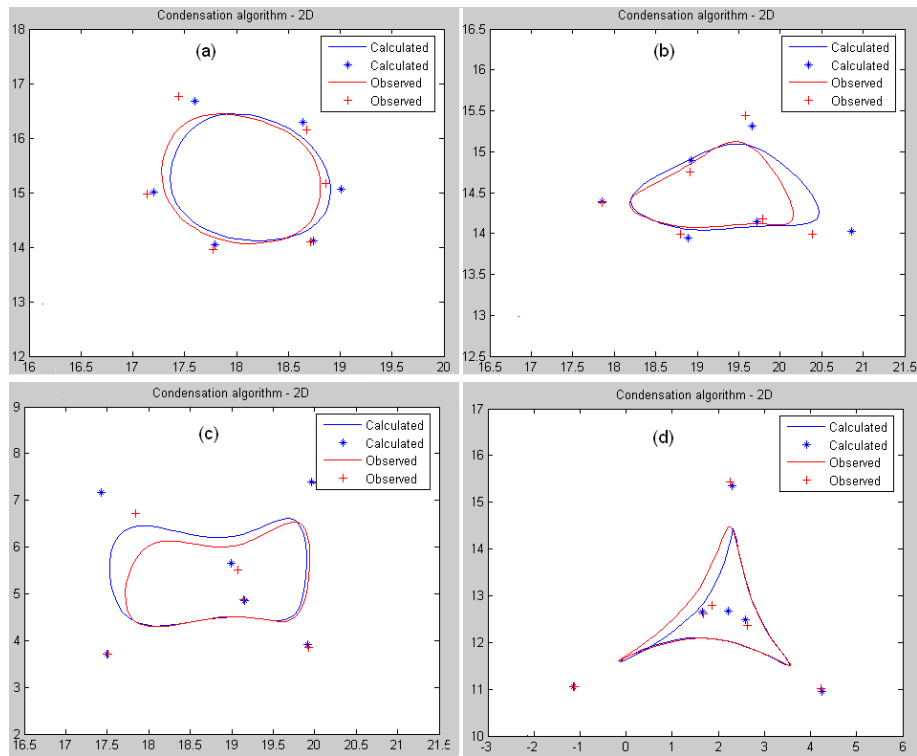


Figure 6.2: This figure contains 4 objects that show the object corner points as observed and as tracked with the help of the condensation algorithm. The shape noise sigma value was 0.1. (a), (b), (c) and (d) are the objects of type 1, 3, 5 and 7 respectively.

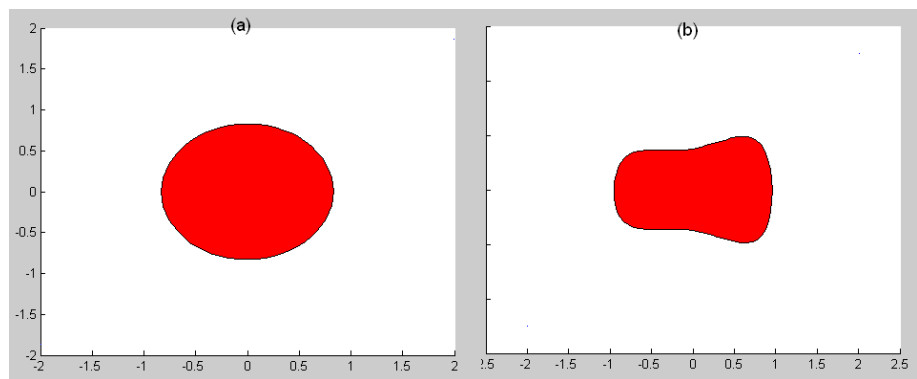


Figure 6.3: This figure consists of 2 sub figures. Each figure has the averaged, B-spline smoothed shape of the object and centroid shifted to the origin. (a) is for object of type 1 and (b) is for the object of type 5.



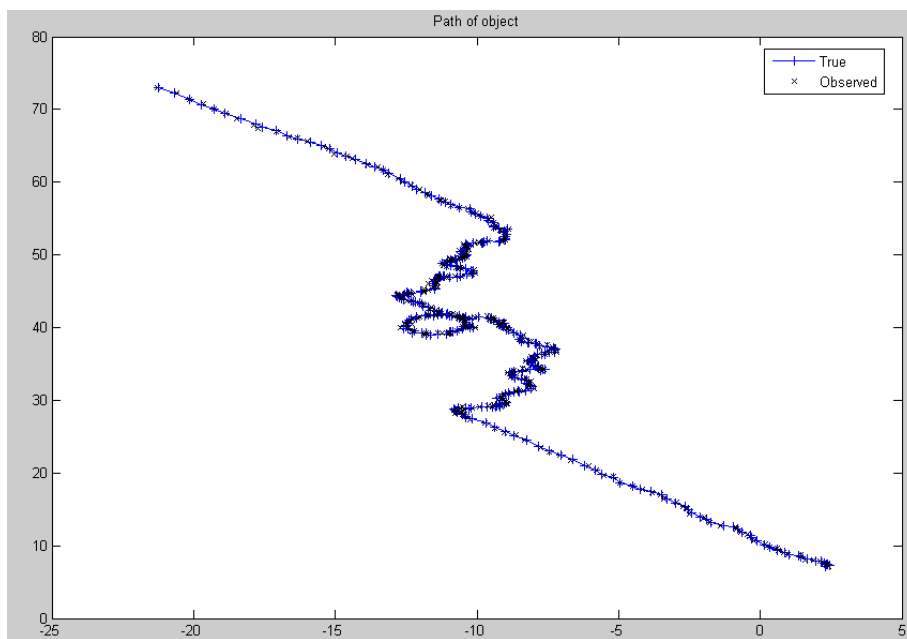


Figure 6.4: This is the path of type 2 which consists of a straight line, a wave, a loop, a wave and a straight line again. The true path is obtained by corrupting ideal values by a noise sigma of 0.075 and the observed values are obtained by corrupting the true path by a noise sigma of 0.05. The observed points are fed to the tracking system.

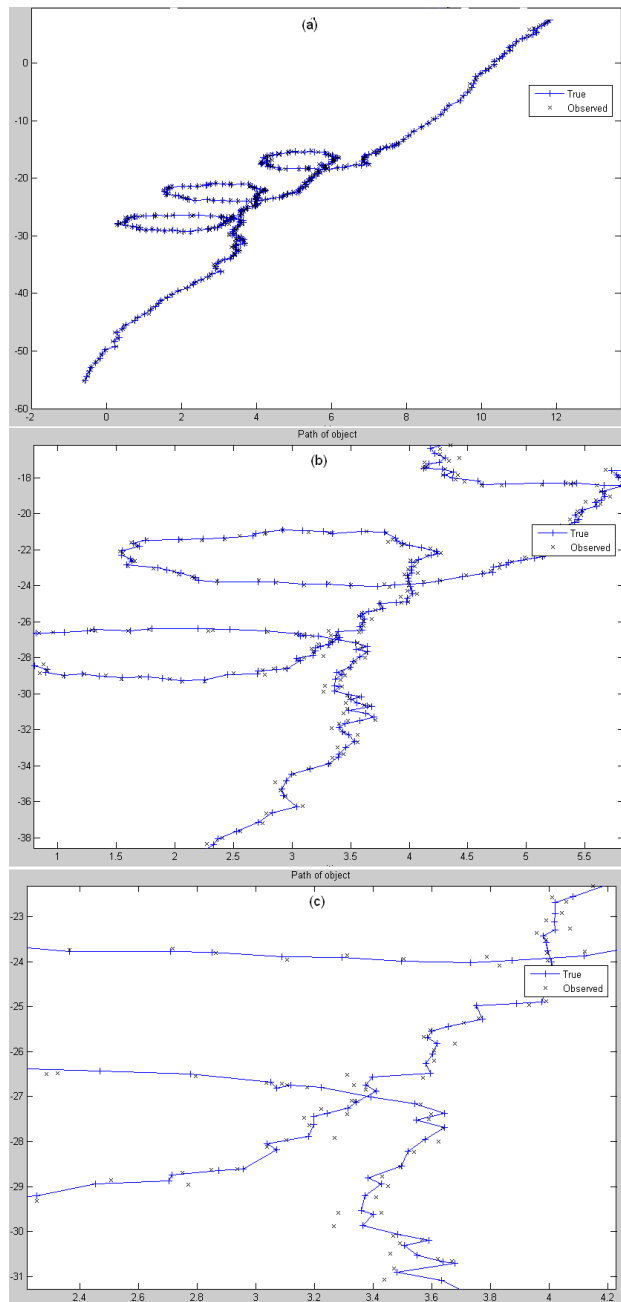


Figure 6.5: This figure of Path type 1 consists of a straight line motion, 3 loops and a straight line motion again. The noise added to the path while creation of the path had a sigma value of 0.075 while the observation noise sigma was 0.05. (a) is the entire path while (b) and (c) are the magnified versions of part of it.

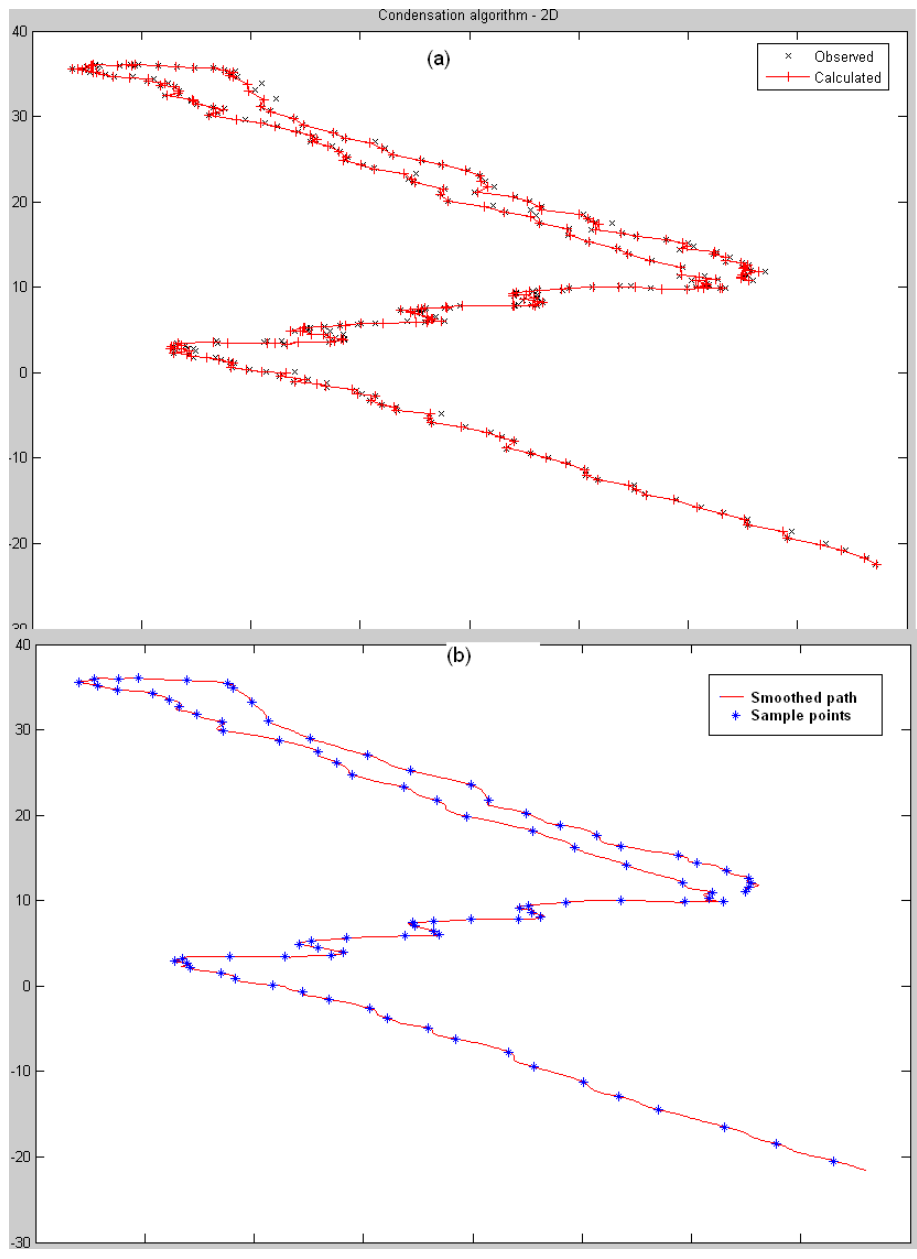


Figure 6.6: This is the path of type 11 that consists of a straight line, a back turn, a straight line, a wave motion and a straight line again. (a) shows the observed values that are fed to the tracker along with the tracked path and (b) shows the path smoothed using B-splines from the output of the tracker system. The blue star points are those sample points used for extracting the behavioral features.

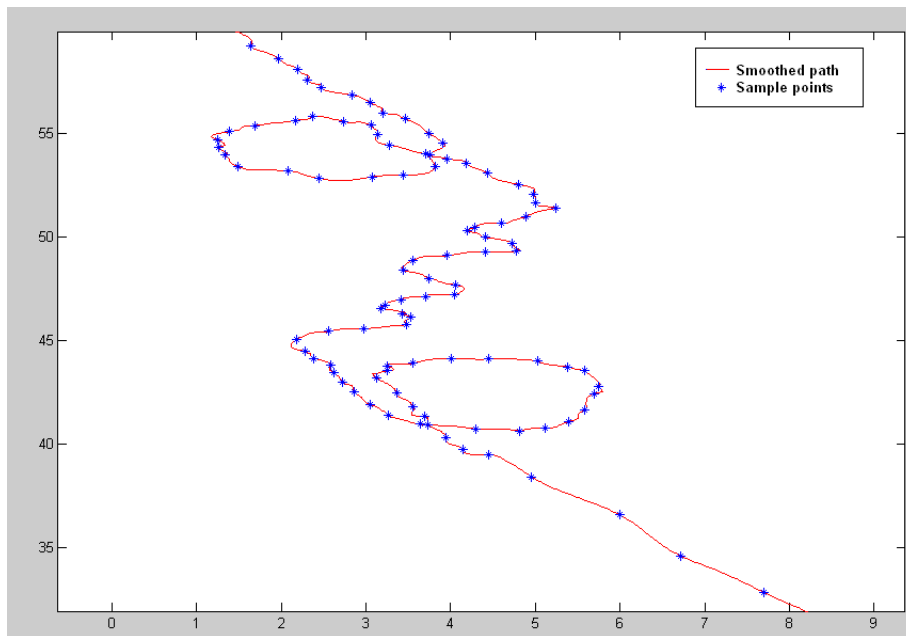


Figure 6.7: This is the path of type 2 which consists of a straight line, a loop, a wave motion, a loop and a straight line motion again. This is the smoothed path obtained after applying the B-spline curves to the output of the path tracked by the condensation algorithm. The blue star points are chosen as samples of the entire path to extract the behavioral features.

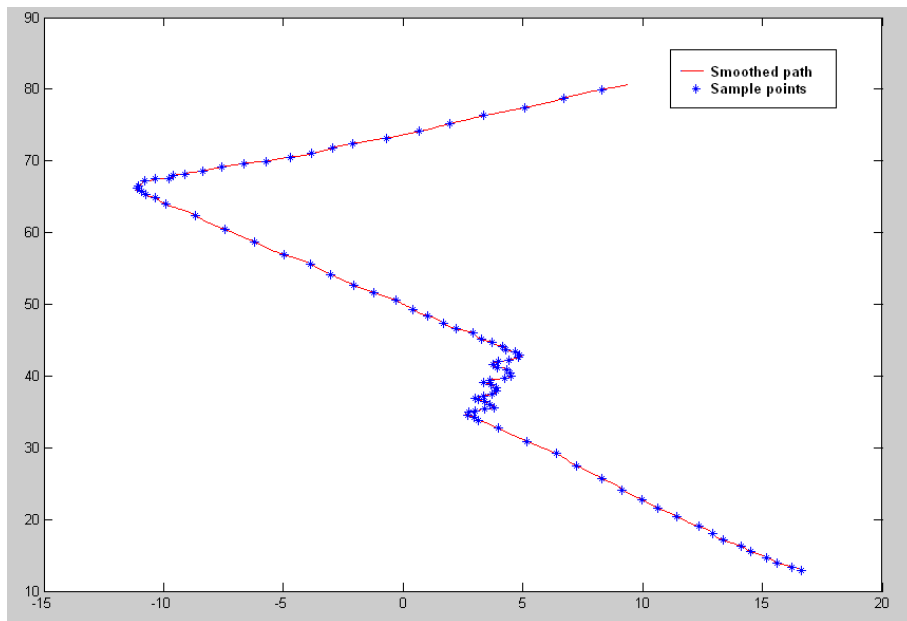


Figure 6.8: This is the path of type 10 which consists of a straight line, a wave motion, a straight line, a right turn and a straight line motion again. This is the smoothed path obtained after applying the B-spline curves to the output of the path tracked by the condensation algorithm. The blue star points are chosen as samples of the entire path to extract the behavioral features.

Table 6.1: Objects type 1, 11, 15, 16, 17, 10 and their path types 1, 2, 3, 4, 5, 6 respectively. The objects are hexagons with size of difference of .01 units and have different behaviors. The training data size was 420 and test data size was 180.

<b>Sr.</b>	<b>Iter</b>	<b>SNS</b>	<b>HN</b>	<b>eta</b>	<b>SA %</b>	<b>BA %</b>
1	4000	0.1	5	0.001	93.889	97.778
2	4000	0.1	5	0.001	92.778	98.333
3	4000	0.1	5	0.001	93.889	98.333
4	10000	0.1	3	0.001	-	98.333
5	10000	0.1	3	0.001	78.333	98.889
6	4000	0.1	7	0.001	93.333	100
7	20000	0.1	7	0.0001	93.333	98.333
8	10000	0.2	5	0.001	76.111	95
9	20000	0.2	3	0.001	73.889	95.556
10	20000	0.2	7	0.001	74.444	93.333

Table 6.2: Objects type 1, 11, 15, 16, 17, 10 and their path types 1, 2, 3, 4, 5, 6 respectively. The objects are hexagons with size of difference of .01 units and have different behaviors. The training data size was 420 and test data size was 180.

<b>Sr.</b>	<b>Iter</b>	<b>SNS</b>	<b>TNS</b>	<b>ONS</b>	<b>SErr</b>	<b>SA %</b>	<b>BErr</b>	<b>BA %</b>
1	420	0.1	0.075	0.05	11	93.89	1	99.44
2	1658	0.2	0.075	0.05	43	76.11	6	96.67
3	660	0.15	0.075	0.05	33	81.67	6	96.67
4	10000	0.25	0.075	0.05	65	63.89	14	92.22
5	1887	0.05	0.075	0.05	0	100.00	1	99.44
6	197	0.1	0.05	0.025	12	93.33	3	98.33
7	244	0.1	0.02	0.02	7	96.11	1	99.44
8	1021	0.1	0.1	0.075	16	91.11	9	95.00

Table 6.3: Objects type 1, 11, 15, 16, 17, 10 and their path types 2, 2, 2, 2, 2, 2 respectively. The objects are hexagons with size of difference of .01 units and have same behaviors. The training data size was 420 and test data size was 180.

Sr.	Iter	SNS	TNS	ONS	SErr	SA %	BErr	BA %
1	1876	0.1	0.075	0.05	7	96.11	9	95.00
2	10000	0.2	0.075	0.05	47	73.89	54	70.00
3	4633	0.15	0.075	0.05	30	83.33	35	80.56
4	10000	0.25	0.075	0.05	59	67.22	68	62.22
5	3230	0.05	0.075	0.05	1	99.44	0	100.00
6	789	0.1	0.05	0.025	11	93.89	16	91.11
7	10000	0.1	0.2	0.2	14	92.22	13	92.78
8	1703	0.1	0.1	0.075	11	93.89	12	93.33

Table 6.4: Objects type 1, 18, 11, 19, 15 and their path types 1, 2, 3, 4, 5 respectively. The objects are hexagons with size of difference of .005 units and have different behaviors. The training data size was 350 and test data size was 150.

Sr.	Iter	SNS	TNS	ONS	SErr	SA %	BErr	BA %
1	526	0.1	0.075	0.05	30	80.00	1	99.33
2	1547	0.2	0.075	0.05	79	47.33	12	92.00
3	536	0.15	0.075	0.05	50	66.67	8	94.67
4	10000	0.25	0.075	0.05	84	44.00	22	85.33
5	409	0.05	0.075	0.05	14	90.67	1	99.33
6	389	0.1	0.05	0.025	28	81.33	2	98.67
7	217	0.1	0.2	0.2	36	76.00	2	98.67
8	3935	0.1	0.1	0.075	38	74.67	15	90.00

Table 6.5: Objects type 1, 18, 11, 19, 15 and their path types 2, 2, 2, 2, 2, 2 respectively. The objects are hexagons with size of difference of .005 units and have the same behaviors. The training data size was 350 and test data size was 150.

Sr.	Iter	SNS	TNS	ONS	SErr	SA %	BErr	BA %
1	20000	0.1	0.075	0.05	36	76.00	38	74.67
2	20000	0.2	0.075	0.05	78	48.00	71	52.67
3	20000	0.15	0.075	0.05	49	67.33	55	63.33
4	20000	0.25	0.075	0.05	79	47.33	79	47.33
5	2212	0.05	0.075	0.05	8	94.67	4	97.33
6	20000	0.1	0.05	0.025	32	78.67	35	76.67
7	20000	0.1	0.2	0.2	35	76.67	35	76.67
8	20000	0.1	0.1	0.075	33	78.00	39	74.00

Table 6.6: Objects type 22, 23, 24, 25 and their path types 5, 6, 7, 8 respectively. The objects are star shapes with a size difference of .01 units and have different behaviors. The training data size was 280 and test data size was 120.

Sr.	Iter	SNS	TNS	ONS	SErr	SA %	BErr	BA %
1	673	0.1	0.075	0.05	43	64.17	2	98.33
2	6448	0.2	0.075	0.05	65	45.83	17	85.83
3	5769	0.15	0.075	0.05	60	50.00	11	90.83
4	20000	0.25	0.075	0.05	73	39.17	32	73.33
5	401	0.05	0.075	0.05	17	85.83	1	99.17
6	340	0.1	0.05	0.025	45	62.50	6	95.00
7	444	0.1	0.2	0.2	42	65.00	2	98.33
8	20000	0.1	0.1	0.075	43	64.17	14	88.33



Table 6.7: Objects type 22, 23, 24, 25 and their path types 7, 7, 7, 7 respectively. The objects are star shapes with a size difference of .01 units and have the same behaviors. The training data size was 280 and test data size was 120.

Sr.	Iter	SNS	TNS	ONS	SErr	SA %	BErr	BA %
1	20000	0.1	0.075	0.05	44	63.33	42	65.00
2	20000	0.2	0.075	0.05	60	50.00	63	47.50
3	20000	0.15	0.075	0.05	54	55.00	58	51.67
4	20000	0.25	0.075	0.05	72	40.00	73	39.17
5	622	0.05	0.075	0.05	8	93.33	15	87.50
6	20000	0.1	0.05	0.025	41	65.83	44	63.33
7	20000	0.1	0.2	0.2	37	69.17	39	67.50
8	20000	0.1	0.1	0.075	42	65.00	40	66.67

Table 6.8: Objects type 20, 21, 3 and their path types 6, 7, 8 respectively. The objects are irregular hexagons with a size difference of .005 units and have different behaviors. The training data size was 210 and test data size was 90.

Sr.	Iter	SNS	TNS	ONS	SErr	SA %	BErr	BA %
1	1802	0.1	0.075	0.05	41	54.44	7	92.22
2	631	0.2	0.075	0.05	54	40.00	11	87.78
3	1976	0.15	0.075	0.05	49	45.56	10	88.89
4	20000	0.25	0.075	0.05	54	40.00	21	76.67
5	242	0.05	0.075	0.05	22	75.56	4	95.56
6	336	0.1	0.05	0.025	37	58.89	1	98.89
7	372	0.1	0.2	0.2	38	57.78	5	94.44
8	250	0.1	0.1	0.075	35	61.11	0	100.00

Table 6.9: Objects type 1, 4, 6, 9, 12, 20, 22 and their path types 2, 3, 4, 5, 6, 7, 8 respectively. The objects have totally different shapes and behaviors. The training data size was 245 and test data size was 105.

<b>Sr.</b>	<b>Iter</b>	<b>SNS</b>	<b>TNS</b>	<b>ONS</b>	<b>SErr</b>	<b>SA %</b>	<b>BErr</b>	<b>BA %</b>
1	308	0.1	0.075	0.05	0	100.00	0	100.00
2	501	0.2	0.075	0.05	0	100.00	0	100.00
3	7727	0.15	0.075	0.05	0	100.00	1	99.05
4	384	0.25	0.075	0.05	0	100.00	1	99.05
5	6405	0.05	0.075	0.05	0	100.00	1	99.05
6	230	0.1	0.05	0.025	0	100.00	1	99.05
7	179	0.1	0.2	0.2	1	99.05	1	99.05
8	742	0.1	0.1	0.075	1	99.05	2	98.10

Table 6.10: Objects type 1, 4, 6, 9, 12, 20, 22 and their path types 4, 4, 4, 4, 4, 4, 4 respectively. The objects have totally different shapes but have the same behavior. The training data size was 245 and test data size was 105.

<b>Sr.</b>	<b>Iter</b>	<b>SNS</b>	<b>TNS</b>	<b>ONS</b>	<b>SErr</b>	<b>SA %</b>	<b>BErr</b>	<b>BA %</b>
1	1003	0.1	0.075	0.05	0	100.00	0	100.00
2	20000	0.2	0.075	0.05	0	100.00	0	100.00
3	4076	0.15	0.075	0.05	0	100.00	2	98.10
4	337	0.25	0.075	0.05	0	100.00	0	100.00
5	625	0.05	0.075	0.05	0	100.00	0	100.00
6	1337	0.1	0.05	0.025	0	100.00	0	100.00
7	1476	0.1	0.2	0.2	0	100.00	0	100.00
8	310	0.1	0.1	0.075	0	100.00	1	99.05

## Chapter 7

# Conclusions and Future work

### 7.1 Conclusions

The goal of this study was to discover if the use of the dynamic content of image sequences coded as behavioral features can aid in object recognition. From the results obtained and shown in the previous chapter we draw the following conclusions:

1. If we are able to define and retrieve the behavioral features reasonably well, and if the characteristic behaviors of similarly appearing object classes are reasonably distinct, then they provide a source of valuable information for object recognition systems.
2. We have favored shape in the above study by choosing objects that are quasi-rigid, i.e. don't change their shape greatly over the entire image sequence. Shape changes are limited to small amounts of noise added to the shape models over time. If the shapes of objects occupying distinct object classes are pretty similar, then a learning system that uses only shape features does not do a very good job. In our experiments, the error rate in such cases was up to 30%. In such cases augmenting the system with behavioral features is more robust against shape changes and exhibits an improved error rate of 5% on an average for our experiments.
3. If we train a system with objects that have very similar shapes as well

as behavioral patterns, then the system which uses both shape and behavior cues may perform worse than the shape-only system. This is likely due to the fact that the behavior features have relatively low information content, with most of their variation due to noise. Thus the added noisy features decrease overall signal to noise ratios and thus performance.

4. The same conclusion can be made about the objects that are reliably and clearly dissimilar in shape and move as rigid bodies with similar behaviors. In this case shape information is sufficient for accurate class recognition. Behavioral information, being of lower quality than shape information, can confuse an otherwise accurate system.

In sum, we conclude that for a range of dynamic object recognition problems, recognition systems cued by both shape and behavioral features are both more accurate and robust. One such class of problems are those in which object shapes are similar or shape is observed with significant random noise or distortion. In circumstances where shapes are quite distinct and clearly observed, behavioral cues are not likely to improve performance noticeably, and may in fact degrade system performance.

## 7.2 Future work

Quite a lot of work can be done in extending the current system. We considered objects that were quasi-rigid and did not change shape radically over time. Variability of shape is prone to degrade a system that relies only on shape features. If such objects have some patterns of movement, they can be used in a combined shape-behavior system for an improved performance. Also, we did not model rotational motion of objects in this proof-of-concept design. Canonical reorientation of objects would result in some noise. This may be simulated to check the effect on the shape and behavioral system. We have not implemented the corner point detection of the objects. We do try to include noise in the system to take care of these effects though. The paths currently are of a standard size so as to be able to be captured in a screen size. Normalization of the paths can be done in future ver-

sions. We may use a hybrid model consisting of a dynamic time warping algorithm, hidden Markov model and a neural network for learning of the behavioral features. We have restricted the number of behavioral features fixed at 5 for the tests done. We can make that variable to accommodate different behavior properties of different objects. Concerning the nature of behavioral features, we can use speed, radius of curvature in turns, and regional loitering time as other behavioral features for a normalized input image sequence. The system can be made smarter by checking to see how the shape-behavioral system does compared to the shape system alone. If the shape system performs better on the validation data we need to use the shape system results else we can rely on the results of the shape and behavioral system.

Finally, the use of behavioral features at more primitive levels, those considered as pre-processing levels in the present study, can be combined with its use as above to explore the full use of behavior in dynamic visual object recognition. In a related study [34] has considered the use of behavior to enhance dynamic segmentation. We propose to collaborate to see the degree to which behavior, exploited both in the early image processing and in the late computer vision stages, impacts the quality of dynamic visual object recognition.

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